

Isabelle/HOL Exercises

Lists

SNOC

Define a primitive recursive function *snoc* that appends an element at the *right* end of a list. Do not use *@* itself.

consts

```
snoc :: "'a list => 'a => 'a list"
```

primrec

```
"snoc [] a = [a]"  
"snoc (x#xs) a = x # snoc xs a"
```

lemma snoc_append: "snoc xs a = xs @ [a]"

```
apply (induct "xs")
```

```
apply auto
```

done

Prove the following theorem:

theorem rev_cons: " $\forall x. \text{rev } (x \# \text{xs}) = \text{snoc } (\text{rev } \text{xs}) \ x$ "

```
apply (induct "xs")
```

```
apply (auto simp add: snoc_append)
```

done

Hint: you need to prove a suitable lemma first.