## Isabelle/HOL Exercises Lists

## **Recursive Functions and Induction: Zip**

Read the chapter about recursive definitions in the "Tutorial on Isabelle/HOL" (*recdef*, Chapter 3.5).

In this exercise you will define a function Zip that merges two lists by interleaving. Examples: Zip [a1, a2, a3] [b1, b2, b3] = [a1, b1, a2, b2, a3, b3] and Zip [a1] [b1, b2, b3] = [a1, b1, b2, b3].

Use three different approaches to define Zip:

- 1. by primitive recursion on the first list,
- 2. by primitive recursion on the second list,
- 3. by total recursion (using recdef).

Show that all three versions of *Zip* are equivalent.

Show that *zipr* distributes over *append*.

lemma "[length p = length u; length q = length v]] ⇒
zipr(p@q,u@v) = zipr(p,u) @ zipr(q,v)"

Note: For *recdef*, the order of your equations is relevant. If equations overlap, they will be disambiguated before they are added to the logic. You can have a look at these equations using *thm zipr.simps*.