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Proseminar Algorithmen und Datenstrukturen

Exercise Sheet 14

Exercise 1 (Depth-first Search)

Given a directed graph G = (V, E) and some node $v \in V$, write a C program that numbers all nodes in the graph according to the order in which they are traversed during depth-first search; the number associated with v should be 1. Make sure that all nodes are numbered, and that all numbers are different! Use adjacency matrices to represent graphs!

See listing dfs_number.c

Exercise 2 (Depth-first Search)

Given a connected, undirected graph G = (V, E), write a C program that computes a spanning tree of G using depth-first search. Use adjacency matrices to represent graphs!

See listing dfs_spantree.c

Exercise 3 (Connected Components)

Given an undirected graph, provide pseudo-code for the computation of its connected components.

Exercise 4 (Connected Components)

Given some node v of an undirected graph, provide pseudo-code for the computation of the number of edges in the connected component v belongs to.

Algorithm 1 Connected components of an undirected graph

Input: *G*: undirected graph

```
begin
component_number := 1
while v is unmarked in G do
    call DFS(v, component_number) /*DFS marking nodes with their comp-nr */
    component_number := component_number + 1
end
```

Algorithm 2 DFS_CountEdges, number of edges in connected component of a node

Input: G: undirected graph, v: some node of G**Output:** twice the number of egdes of the component v belongs to

 $\begin{array}{l} \mathbf{begin} \\ \mathrm{mark}(v) \\ \mathbf{for} \; \mathrm{each} \; w \; \mathrm{adjacent} \; \mathrm{to} \; v \; \mathbf{do} \\ edgecount := edgecount + 1 \\ \mathbf{if} \; w \; \mathrm{is} \; \mathrm{unmarked} \; \mathbf{then} \\ \quad \mathbf{call} \; DFS_CountEdges(G,w) \\ \mathbf{end} \end{array}$