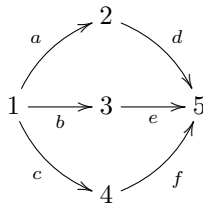


Homework

1. Encode a (linear) polynomial interpretation showing termination of the rule $f(f(x)) \rightarrow f(g(f(x)))$ in NIA. Is the constraint satisfiable? What does MiniSmt reply?

Hint: Use abstract interpretations $f_{\mathbb{N}}(x) = f_1x + f_0$ and $g_{\mathbb{N}}(x) = g_1x + g_0$.

2. Consider the weighted graph:



Perform the *state elimination algorithm* eliminating nodes

- a) 1,2,3,4,5
- b) 2,3,4,1,5

Conclude a strategy to obtain *small* intermediate graphs and hence small formulas.

3. Decide the satisfiability of the following quantifier-free formulas in the theory of arrays:

- (a) $a\langle i \triangleleft e \rangle[j] = e \wedge a[j] \neq e$
- (b) $i_1 = j \wedge a[j] = v_1 \wedge a\langle i_1 \triangleleft v_1 \rangle\langle i_2 \triangleleft v_2 \rangle[j] \neq a[j]$

4. Decide the satisfiability of the following formulas:

- (a) $a[k] = b[k] \wedge \forall i a[i] = b[i]$
- (b) $\forall i \forall j (\ell \leq i \leq j \leq u \rightarrow a[i] \leq a[j]) \wedge a[\ell] > a[u]$