

1. *Solution.* % graph  $G$

```
edge(a,b).
edge(a,c).
edge(b,d).
edge(c,d).
edge(d,e).
edge(f,g).
```

% *connected*( $X,Y$ ) is true if  $X$  is connected to  $Y$  in  $G$   
%

```
connected(X,X).
connected(X,Z) :-
    edge(X,Y),
    connected(Y,Z).
```

We show that the size of the search tree is (grossly) bounded by  $O(n^2)$ , where  $n$  is the number of vertices in the graph  $G$ . First, we observe that the number of edges in a graph with  $n$  nodes is bounded by  $n^2$ . Furthermore, in searching for a connection we need to consider each edge at most once. Hence the search tree is bounded by  $O(n^2)$ . This argument is independent of the fact that the goal is ground or not.  $\square$

2. *Solution.*

```
duplicate(Xs,N,Ys) :-
    duplicate2(Xs,N,Ys \ []).

duplicate2([],_N,Ys\Ys).
duplicate2([X|Xs],N,Ys0\Ys2) :-
    generate(X,N,Ys0\Ys1),
    duplicate2(Xs,N,Ys1\Ys2).

generate(_X,0,Ys\Ys).
generate(X,N,Ys0\Ys1) :-
    N > 0,
    N1 is N - 1,
    generate(X,N1,Ys0\[X|Ys1]).
```

$\square$

3. *Solution.*

```

isotree(nil, nil).
isotree(tree(X, Left1, Right1), tree(X, Left2, Right2)) :-
    isotree(Left1, Left2),
    isotree(Right1, Right2).
isotree(tree(X, Left1, Right1), tree(X, Left2, Right2)) :-
    isotree(Left1, Right2),
    isotree(Right1, Left2).

```

□

#### 4. Solution.

```

% prop/1 —> DCG that generates well-parenthesised propositional formulas
% and stores the syntax tree
%
prop(true) —> "true".
prop(false) —> "false".
prop(not(A)) —> "not", prop(A).
prop(and(A,B)) —> "(", prop(A), "and", prop(B), ")".
prop(or(A,B)) —> "(", prop(A), "or", prop(B), ")".

% prop2/1 —> DCG that generates propositional formulas using
% the standard precedence
%
atom(p) —> "true".
atom(q) —> "false".
atom(A) —> "(", prop2(A), ")".
unary(not(A)) —> "not", unary(A).
unary(A) —> atom(A).
and(and(A,B)) —> unary(A), "and", and(B).
and(A) —> unary(A).
prop2(or(A,B)) —> and(A), "or", or(B).
prop2(A) —> and(A).

```

□

#### 5. Solution.

```

jump(N,A/B,C/D) :-
    jump_dist(X,Y),
    C is A+X, C > 0, C =< N,
    D is B+Y, D > 0, D =< N.

jump_dist(1,2).
jump_dist(2,1).
jump_dist(2,-1).

```

```

jump_dist(1,-2).
jump_dist(-1,-2).
jump_dist(-2,-1).
jump_dist(-2,1).
jump_dist(-1,2).

```

□

## 6. *Solution.*

statement	yes	no
A rule is a universally quantified logical formula of the form $A \leftarrow B_1, B_2, \dots, B_n$ , where $A$ is a goal and for all $i = 1, \dots, n$ : $B_i$ is a goal.	<input checked="" type="checkbox"/>	<input type="checkbox"/>
An SLD-refutation is a finite SLD-derivation ending in the goal to be proven.	<input type="checkbox"/>	<input checked="" type="checkbox"/>
Logic programming is a declarative programming paradigm, that is, the computation of a function is made a first-class citizen.	<input type="checkbox"/>	<input checked="" type="checkbox"/>
The declarative semantics of a program $P$ is the minimal model of $P$ .	<input checked="" type="checkbox"/>	<input type="checkbox"/>
The order of goals is irrelevant in the computation model of logic programming, but not the order of rules.	<input checked="" type="checkbox"/>	<input type="checkbox"/>
A search tree is the same as an SLD tree.	<input checked="" type="checkbox"/>	<input type="checkbox"/>
Prolog is a language without types and the main technique to manipulate data is unification.	<input checked="" type="checkbox"/>	<input type="checkbox"/>
Difference lists are ineffective if the generation of different sections of a list depend on each other.	<input checked="" type="checkbox"/>	<input type="checkbox"/>
A meta-interpreter in Prolog interprets Prolog terms on the Warren abstract machine.	<input type="checkbox"/>	<input checked="" type="checkbox"/>
The predicate $bagof(Template, Goal, Bag)$ unifies $Bag$ with the alternatives of $Goal$ that meet $Template$ .	<input type="checkbox"/>	<input checked="" type="checkbox"/>

□