

# Logic Programming

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#### Summary of Last Lecture

# Outline of the Lecture

## Logic Programs

introduction, basic constructs, database and recursive programming, theory of logic programs

## The Prolog Language

programming in pure prolog, arithmetic, structure inspection, meta-logical predicates, cuts, extra-logical predicates, how to program efficiently

# Advanced Prolog Programming Techniques

nondeterministic programming, incomplete data structures, definite clause grammars, meta-programming , constraint logic programming

# Summary of Last Lecture

# Two Choices

- 1 goal in sequence of goals
- 2 rule in logic program

substitution

avoid choice by always taking mgu

## Computation Model of Logic Programs

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- the choice of goal is arbitrary if there is a successful computation for a specific order, then there is a successful computation for any other order
- the choice of rules is essential not every choice will lead to a successful computation; thus the computation model is nondeterministic

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35/

Making Implicit Information Exp

# Database Programming

## Example

father(andreas,boris).	<pre>female(doris).</pre>	male(andreas).
father(andreas,christian).	female(eva).	male(boris).
father(andreas,doris).		male(christian).
father(boris,eva).	<pre>mother(doris,franz).</pre>	male(franz).
<pre>father(franz,georg).</pre>	<pre>mother(eva,georg).</pre>	<pre>male(georg).</pre>

# Naming Conventions

- predicates are often denoted together with their arity: father/2
- for each predicate a relation scheme is defined: father, Child)
- relation schemes are denoted in italics
- variables should have mnemonic names; each new word in a variable is started with a capital letter: *NieceOrNephew*
- in predicates words are separated by underscores: *schedule\_conflict*

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• relation schemes are also used in commenting code

#### Making Implicit Information Explic

Example

### **Relation Schemes**

daughter(Daughter,Parent) parent(Parent,Child) grandfather(Grandfather,GrandChild)

Example

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#### Database Programming

Making Implicit Information Explicit

## Structured Data and Data Abstraction

Example (Unstructured Data)

```
course(discrete_mathematics,tuesday,8,11,sandor,szedmak,
    victor_franz_hess,d).
```

## Example (Structured Data)

course(discrete\_mathematics,time(tuesday,8,11), lecturer(sandor,szedmak),location(victor\_franz\_hess,d)).

### Example

40/1

## Example

```
andreas ≠ boris. andreas ≠ georg. ...
andreas ≠ christian. boris ≠ christian.
andreas ≠ franz. boris ≠ franz.
brother(Brother,Sib) ←
    parent(Parent,Brother), parent(Parent,Sib),
    male(Brother), Brother ≠ Sib.
```

### Example

 $mother(Woman) \leftarrow mother(Woman, Child).$ 

### Observation

overloading with the same predicate name, but different arity, is fine

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## Example (cont'd)

```
occupied(Location,Day,Time) ←
  course(Course,time(Day,Start,Finish),Lecturer,Location),
  Start ≤ Time, Time ≤ Finish.
```

### Why structure Data?

- helps to organise data
- rules can be written abstractly, hiding irrelevant detail
- modularity is improved

### The Art of Prolog says

We believe that the appearance of a program is important, particularly when attempting difficult problems

#### Making Implicit Information Explicit

## **Recursive Rules**

### Example

```
grandpartent(Ancestor,Descendant) ~
parent(Ancestor,Person), parent(Person,Descendant).
greatgrandpartent(Ancestor,Descendant) ~
parent(Ancestor,Person), grandpartent(Person,Descendant).
greatgreatgrandpartent(Ancestor,Descendant) ~
```

```
parent(Ancestor,Person), greatgrandpartent(Person,Descendant)
:
```

## Example

```
\texttt{ancestor}(\texttt{Ancestor},\texttt{Descendant}) \ \leftarrow
```

```
parent(Ancestor,Person), ancestor(Person,Descendant).
```

```
\verb+ancestor(Ancestor,Descendent) \ \leftarrow \ \verb+parent(Ancestor,Descendent).
```

```
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```

#### Recursive Programming

# **Recursive Programming**

### Definition

- a type is a (possible infinite) set of terms
- types are conveniently defined by unary relations

### Example

male(X). female(X).

### Definition

- to define complex types, recursive logic programs may be necessary
- the latter types are called recursive types
- recursive types, defined by unary recursive programs, are called simple recursive types
- a program defining a type is a type definition; a call to a predicate defining a type is a type condition

# Logic Programs and the Relational Database Model

### Observation

the basic operations of relational algebras, namely:

- 1 union
- 2 difference
- 3 cartesian product
- 4 projection
- 5 selection
- 6 intersection

can easily be expressed within logic programming

## Example

 $r\_union\_s(X_1,\ldots,X_n) \leftarrow r(X_1,\ldots,X_n).$  $r\_union\_s(X_1,\ldots,X_n) \leftarrow s(X_1,\ldots,X_n).$ 

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43/1

#### Recursive Programming

# Simple Recursive Types

### Example

```
is_tree(nil).
is_tree(tree(Element,Left,Right)) 
is_tree(Left),
is_tree(Right).
```

### Definition

- a type is complete if closed under the instance relation
- with every complete type *T* one associates an incomplete type *IT* which is a set of terms with instances in *T* and instances not in *T*

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### Example

- the type  $\{0, s(0), s(s(0)), ...\}$  is complete
- the type  $\{X, 0, s(0), s(s(0)), \dots\}$  is incomplete

## Arithmetic

### Example

```
natural_number(0).
natural_number(s(X)) \leftarrow natural_number(X).
```

## Example

## Example

```
\begin{array}{l} \texttt{factorial(0,s(0)).} \\ \texttt{factorial(s(N),F)} \ \leftarrow \ \texttt{factorial(N,F_1), \ times(s(N),F_1,F).} \end{array}
```

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46,

#### Recursive Programming

## Lists

### Notation

• []	empty list		
• [ <i>H</i>   <i>T</i> ]	list with head $H$ and tail $T$		
• [A]	[A []]	list with one element	
• [A,B]	[A [B []]]	list with two elements	
• [A,B T]	[A [B T]]	list with at least two elements	

## Example

 $is_list([]). is_list([X|Xs]) \leftarrow is_list(Xs).$ 

## Notation (cont'd)

formal object	cons pair syntax	element syntax		
.(a,[])	[a []]	[a]		
.(a,.(b,[]))	[a [b []]]	[a,b]		

#### ecursive Programming

### Example

#### Example

#### Example

ackermann(0,N,s(N)).
ackermann(s(M),0,Val) ← ackermann(M,s(0),Val).
ackermann(s(M),s(N),Val) ← ackermann(s(M),N,Val<sub>1</sub>),
ackermann(M,Val<sub>1</sub>,Val).

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47/2

#### Recursive Programming

Example	
<pre>member(X,[X Xs]).</pre>	
$member(X,[Y Xs]) \leftarrow member(X,Xs).$	$\leftarrow \texttt{member(X,[a,b,a])}.$

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### Example append(Xs,Ys,Zs) ←

Xs = [], Zs = Ys. append(Xs,Ys,Zs) ← Xs = [H|Ts], append(Ts,Ys,Us), Zs = [H|Us]. append([],Ys,Ys).
append([H|Ts],Ys,[H|Zs]) ←
append(Ts,Ys,Zs).

```
Example
```

```
prefix([],Xs).
prefix([X|Xs],[X|Ys]) ←
    prefix(Xs,Ys).
```

suffix(Xs,Xs). $suffix(Xs,[Y|Ys]) \leftarrow$ suffix(Xs,Ys).

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```
Example (Uses of append)
```

### Example

```
reverse([],[]).
reverse([X|Xs],Zs) ~ reverse(Xs,Ys), append(Ys,[X],Zs).
reverse([X|Xs],Acc,Ys) ~ reverse(Xs,[],Ys).
reverse([X|Xs],Acc,Ys) ~ reverse(Xs,[X|Acc],Ys).
reverse([],Ys,Ys).
```

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### Example

```
length([],0).\\length([X|Xs],s(N)) \leftarrow length(Xs,N).
```

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#### Composing Recursive Programs

### Example

```
\begin{array}{l} \texttt{delete}_2([\texttt{X}|\texttt{Xs}],\texttt{X},\texttt{Ys}) \leftarrow \texttt{delete}_2(\texttt{Xs},\texttt{X},\texttt{Ys}).\\ \texttt{delete}_2([\texttt{X}|\texttt{Xs}],\texttt{Z},[\texttt{X}|\texttt{Ys}]) \leftarrow \texttt{delete}_2(\texttt{Xs},\texttt{Z},\texttt{Ys}).\\ \texttt{delete}_2([],\texttt{X},[]).\\ \leftarrow \texttt{delete}_2([a,b,c,b],b,[a,c])\\ \texttt{true}\\ \leftarrow \texttt{delete}_2([a,b,c,b],b,[a,b,c,d])\\ \texttt{true}\end{array}
```

### Example

# Composing Recursive Programs

### Example

delete/3 removes all occurrences of an element from a list

### Approach

- 1 craft the predicate with one (procedural) use in mind
- **2** afterwards see, if alternative uses make declarative sense

#### Example

```
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```

51/

#### Sorting

### Example

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### Example

## Example

```
quicksort([X|Xs],Ys) ←
partition(Xs,X,Littles,Bigs),
quicksort(Littles,Ls), quicksort(Bigs,Rs),
append(Ls,[X|Rs],Ys).
partition([X|Xs],Y,[X|Ls],Bs) ←
X =< Y, partition(Xs,Y,Ls,Bs).
partition([X|Xs],Y,Ls,[X|Bs]) ←
X > Y, partition(Xs,Y,Ls,Bs).
partition([],Y,[],[]).
```

Example (Recursive Datastructures)

isotree(nil,nil).

```
isotree(tree(X,Left1,Right1),tree(X,Left2,Right2)) ←
    isotree(Left1,Left2), isotree(Right1,Right2).
isotree(tree(X,Left1,Right1),tree(X,Left2,Right2)) ←
    isotree(Left1,Right2), isotree(Right1,Left2).
```

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54/1