



Logic

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Outline

1. Summary of Previous Lecture
2. Adequacy
3. Evaluation
4. Fairness
5. Intermezzo
6. LTL Model Checking Algorithm
7. Further Reading
8. Exam

Definitions

model $\mathcal{M} = (S, \rightarrow, L)$ and $X \subseteq S$

- $\llbracket \varphi \rrbracket = \{s \in S \mid \mathcal{M}, s \models \varphi\}$
- $\text{pre}_\forall(X) = \{s \in S \mid t \in X \text{ for all } t \text{ with } s \rightarrow t\}$
- $\text{pre}_\exists(X) = \{s \in S \mid s \rightarrow t \text{ for some } t \in X\}$

Lemma

$\llbracket \top \rrbracket = S$	$\llbracket p \rrbracket = \{s \in S \mid p \in L(s)\}$
$\llbracket \perp \rrbracket = \emptyset$	$\llbracket \text{AX } \varphi \rrbracket = \text{pre}_\forall(\llbracket \varphi \rrbracket)$
$\llbracket \neg \varphi \rrbracket = S - \llbracket \varphi \rrbracket$	$\llbracket \text{EX } \varphi \rrbracket = \text{pre}_\exists(\llbracket \varphi \rrbracket)$
$\llbracket \varphi \wedge \psi \rrbracket = \llbracket \varphi \rrbracket \cap \llbracket \psi \rrbracket$	$\llbracket \text{AF } \varphi \rrbracket = \llbracket \varphi \rrbracket \cup \text{pre}_\forall(\llbracket \text{AF } \varphi \rrbracket)$
$\llbracket \varphi \vee \psi \rrbracket = \llbracket \varphi \rrbracket \cup \llbracket \psi \rrbracket$	$\llbracket \text{EF } \varphi \rrbracket = \llbracket \varphi \rrbracket \cup \text{pre}_\exists(\llbracket \text{EF } \varphi \rrbracket)$
$\llbracket \varphi \rightarrow \psi \rrbracket = (S - \llbracket \varphi \rrbracket) \cup \llbracket \psi \rrbracket$	$\llbracket \text{AG } \varphi \rrbracket = \llbracket \varphi \rrbracket \cap \text{pre}_\forall(\llbracket \text{AG } \varphi \rrbracket)$
$\text{pre}_\forall(X) = S - \text{pre}_\exists(S - X)$	$\llbracket \text{EG } \varphi \rrbracket = \llbracket \varphi \rrbracket \cap \text{pre}_\exists(\llbracket \text{EG } \varphi \rrbracket)$
	$\llbracket \text{A}[\varphi \cup \psi] \rrbracket = \llbracket \psi \rrbracket \cup (\llbracket \varphi \rrbracket \cap \text{pre}_\forall(\llbracket \text{A}[\varphi \cup \psi] \rrbracket))$
	$\llbracket \text{E}[\varphi \cup \psi] \rrbracket = \llbracket \psi \rrbracket \cup (\llbracket \varphi \rrbracket \cap \text{pre}_\exists(\llbracket \text{E}[\varphi \cup \psi] \rrbracket))$

Lemma

- $\llbracket \text{AF } \varphi \rrbracket$ is least fixed point of monotone function $F_{\text{AF}}(X) = \llbracket \varphi \rrbracket \cup \text{pre}_{\forall}(X)$
- $\llbracket \text{EG } \varphi \rrbracket$ is greatest fixed point of monotone function $F_{\text{EG}}(X) = \llbracket \varphi \rrbracket \cap \text{pre}_{\exists}(X)$
- $\llbracket \text{E}[\psi \cup \varphi] \rrbracket$ is least fixed point of monotone function $F_{\text{EU}}(X) = \llbracket \psi \rrbracket \cup (\llbracket \varphi \rrbracket \cap \text{pre}_{\exists}(X))$

Theorem (Knaster–Tarski)

every monotone function $F: \mathcal{P}(S) \rightarrow \mathcal{P}(S)$ with $|S| = n$ admits

- least fixed point $\mu F = F^n(\emptyset)$
- greatest fixed point $\nu F = F^n(S)$

symbolic model checking = (CTL) model checking with BDDs

Definition

LTL formulas φ and ψ are **semantically equivalent** ($\varphi \equiv \psi$) if

$$\pi \models \varphi \iff \pi \models \psi$$

for all models $\mathcal{M} = (S, \rightarrow, L)$ and paths π in \mathcal{M}

Remark

$$\pi \not\models \varphi \iff \pi \models \neg \varphi \quad \mathcal{M}, s \models \varphi \implies \mathcal{M}, s \not\models \neg \varphi \quad \mathcal{M}, s \not\models \varphi \not\Rightarrow \mathcal{M}, s \models \neg \varphi$$

Definitions

- **LTL (linear-time temporal logic)** formulas are built from
 - atoms p, q, r, p_1, p_2, \dots
 - logical connectives $\perp, \top, \neg, \wedge, \vee, \rightarrow$
 - temporal connectives X, F, G, U, W, R
- according to following BNF grammar:
- $$\begin{aligned} \varphi ::= & \perp \mid \top \mid p \mid (\neg \varphi) \mid (\varphi \wedge \varphi) \mid (\varphi \vee \varphi) \mid (\varphi \rightarrow \varphi) \mid \\ & (X \varphi) \mid (F \varphi) \mid (G \varphi) \mid (\varphi U \varphi) \mid (\varphi W \varphi) \mid (\varphi R \varphi) \end{aligned}$$
- **path** in model $\mathcal{M} = (S, \rightarrow, L)$ is infinite sequence $s_1 \rightarrow s_2 \rightarrow \dots$
 - **satisfaction** $\pi \models \varphi$ of LTL formula φ with respect to path $\pi = s_1 \rightarrow s_2 \rightarrow \dots$ in model \mathcal{M} is defined by induction on φ
 - **satisfaction** $\mathcal{M}, s \models \varphi$ of LTL formula φ with respect to state $s \in S$ in model \mathcal{M} is defined as "for all paths $\pi = s \rightarrow \dots \pi \models \varphi$ "

Theorem

$$\begin{array}{ll} \neg X \varphi \equiv X \neg \varphi & \varphi U \psi \equiv \neg(\neg \psi U (\neg \varphi \wedge \neg \psi)) \wedge F \psi \\ \neg F \varphi \equiv G \neg \varphi & F(\varphi \vee \psi) \equiv F \varphi \vee F \psi \\ \neg G \varphi \equiv F \neg \varphi & G(\varphi \wedge \psi) \equiv G \varphi \wedge G \psi \\ \neg(\varphi U \psi) \equiv \neg \varphi R \neg \psi & F \varphi \equiv \top U \varphi \\ \neg(\varphi R \psi) \equiv \neg \varphi U \neg \psi & G \varphi \equiv \perp R \varphi \\ \varphi U \psi \equiv \varphi W \psi \wedge F \psi & \varphi W \psi \equiv \psi R (\varphi \vee \psi) \\ \varphi W \psi \equiv \varphi U \psi \vee G \varphi & \varphi R \psi \equiv \psi W (\varphi \wedge \psi) \end{array}$$

Part I: Propositional Logic

algebraic normal forms, binary decision diagrams, conjunctive normal forms, DPLL, Horn formulas, natural deduction, Post's adequacy theorem, resolution, SAT, semantics, sorting networks, soundness and completeness, syntax, Tseitin's transformation

Part II: Predicate Logic

natural deduction, quantifier equivalences, resolution, semantics, Skolemization, syntax, undecidability, unification

Part III: Model Checking

adequacy, branching-time temporal logic, CTL*, fairness, linear-time temporal logic, model checking algorithms, symbolic model checking

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1. Summary of Previous Lecture

2. Adequacy

LTL CTL

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Theorem

$\{X, U\}$, $\{X, W\}$ and $\{X, R\}$ are adequate sets of temporal connectives for LTL

Proof

$$\begin{array}{lll} F\varphi \equiv T \cup \varphi & \varphi R \psi \equiv \psi W(\varphi \wedge \psi) & \varphi U \psi \equiv \neg(\neg \varphi R \neg \psi) \\ G\varphi \equiv \neg F \neg \varphi & \varphi U \psi \equiv \neg(\neg \varphi R \neg \psi) & F\varphi \equiv T \cup \varphi \\ \varphi R \psi \equiv \neg(\neg \varphi U \neg \psi) & F\varphi \equiv T \cup \varphi & G\varphi \equiv \neg F \neg \varphi \\ \varphi W \psi \equiv \varphi U \psi \vee G\varphi & G\varphi \equiv \neg F \neg \varphi & \varphi W \psi \equiv \varphi U \psi \vee G\varphi \end{array}$$

Theorem

$\{U, R\}$, $\{U, W\}$, $\{U, G\}$, $\{F, W\}$ and $\{F, R\}$ are adequate sets of temporal connectives for LTL fragment consisting of negation-normal forms without X

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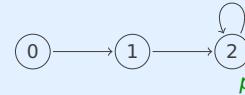
Theorem

set of temporal connectives is adequate for CTL \iff

$$\text{it contains } \begin{cases} \text{at least one of } \{\text{AX, EX}\} \\ \text{at least one of } \{\text{EG, AF, AU}\} \\ \text{EU} \end{cases}$$

Proof (\Leftarrow)

- $\text{AX } \varphi \equiv \neg \text{EX } \neg \varphi$ and $\text{EX } \varphi \equiv \neg \text{AX } \neg \varphi$
- $\text{EF } \varphi \equiv E[\top \cup \varphi]$
- $\text{AG } \varphi \equiv \neg \text{EF } \neg \varphi$
- $\text{A}[\varphi \cup \psi] \equiv \neg(E[\neg \psi \cup (\neg \varphi \wedge \neg \psi)] \vee \text{EG } \neg \psi)$
- $\text{AF } \varphi \equiv A[\top \cup \varphi]$
- $\text{EG } \varphi \equiv \neg \text{AF } \neg \varphi$



Proof (\Rightarrow , cont'd)

induction on φ

- if φ is atom or $\varphi = \perp$ then $\mathcal{M}, 0 \not\models \varphi$ and $\mathcal{M}, 1 \not\models \varphi$
- if $\varphi = \top$ then $\mathcal{M}, 0 \models \varphi$ and $\mathcal{M}, 1 \models \varphi$
- if $\varphi = \neg \psi$ then $\mathcal{M}, 0 \models \varphi \iff \mathcal{M}, 0 \not\models \psi \iff \mathcal{M}, 1 \not\models \psi \iff \mathcal{M}, 1 \models \varphi$
- if $\varphi = \psi_1 \wedge \psi_2$ then

$$\begin{aligned} \mathcal{M}, 0 \models \varphi &\iff \mathcal{M}, 0 \models \psi_1 \text{ and } \mathcal{M}, 0 \models \psi_2 \\ &\iff \mathcal{M}, 1 \models \psi_1 \text{ and } \mathcal{M}, 1 \models \psi_2 \iff \mathcal{M}, 1 \models \varphi \end{aligned}$$

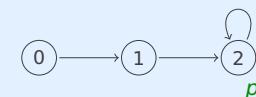
Theorem

set of temporal connectives is adequate for CTL \iff

$$\text{it contains } \begin{cases} \text{at least one of } \{\text{AX, EX}\} \\ \text{at least one of } \{\text{EG, AF, AU}\} \\ \text{EU} \end{cases}$$

Proof (\Rightarrow)

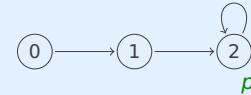
- consider model \mathcal{M}



- $\mathcal{M}, 0 \not\models \text{EX } p$ and $\mathcal{M}, 1 \models \text{EX } p$

- for every CTL formula φ not containing EX and AX:

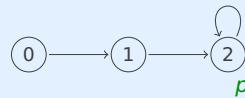
$$\mathcal{M}, 0 \models \varphi \iff \mathcal{M}, 1 \models \varphi$$



Proof (\Rightarrow , cont'd)

induction on φ

- if $\varphi = \text{AF } \psi$ or $\varphi = \text{EF } \psi$ then
$$\begin{aligned} \mathcal{M}, 0 \models \varphi &\iff \mathcal{M}, i \models \psi \text{ for some } i \in \{0, 1, 2\} \\ &\iff \mathcal{M}, i \models \psi \text{ for some } i \in \{1, 2\} \iff \mathcal{M}, 1 \models \varphi \end{aligned}$$
- if $\varphi = \text{AG } \psi$ or $\varphi = \text{EG } \psi$ then
$$\begin{aligned} \mathcal{M}, 0 \models \varphi &\iff \mathcal{M}, i \models \psi \text{ for all } i \in \{0, 1, 2\} \\ &\iff \mathcal{M}, i \models \psi \text{ for all } i \in \{1, 2\} \iff \mathcal{M}, 1 \models \varphi \end{aligned}$$



Proof (\Rightarrow , cont'd)

induction on φ

- if $\varphi = A[\psi_1 \cup \psi_2]$ or $\varphi = E[\psi_1 \cup \psi_2]$ then

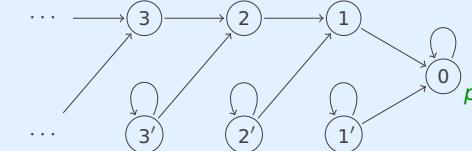
$$\begin{aligned} M, 0 \models \varphi &\iff M, 0 \models \psi_2 \text{ or} \\ &M, 1 \models \psi_2 \text{ and } M, 0 \models \psi_1 \text{ or} \\ &M, 2 \models \psi_2 \text{ and } M, 0 \models \psi_1 \text{ and } M, 1 \models \psi_1 \\ &\iff M, 1 \models \psi_2 \text{ or} \\ &M, 2 \models \psi_2 \text{ and } M, 1 \models \psi_1 \\ &\iff M, 1 \models \varphi \end{aligned}$$

Theorem

... at least one of {EG, AF, AU}

Proof (\Rightarrow)

- consider model M



- $M, i \models AF p$ for all $i \geq 0$ and $M, i' \not\models AF p$ for all $i > 0$
- for every CTL formula φ not containing EG, AF and AU there exists $n_\varphi > 0$ such that

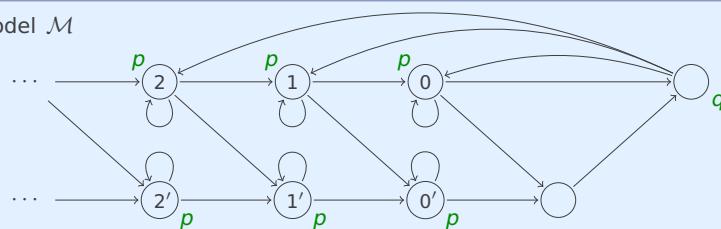
$$M, n_\varphi \models \varphi \iff M, n'_\varphi \models \varphi$$

Theorem

... EU

Proof (\Rightarrow)

- consider model M



- $M, i \models E[p \cup q]$ and $M, i' \not\models E[p \cup q]$ for all $i \geq 0$
- for every CTL formula φ not containing EU there exists $n_\varphi \geq 0$ such that

$$M, n_\varphi \models \varphi \iff M, n'_\varphi \models \varphi$$

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Online Evaluation in Presence

<https://lv-analyse.uibk.ac.at/evasys/public/online/index>



Motivation

- ▶ model may contain behaviour which is unrealistic or guaranteed not to happen
- ▶ such behaviour is (typically) not expressible in CTL
- ▶ eliminate such behaviour by imposing **fairness constraints**

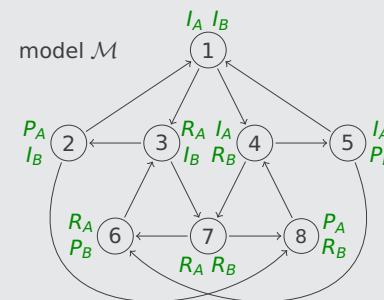
Definitions

- ▶ path $s_1 \rightarrow s_2 \rightarrow \dots$ is **fair** with respect to set C of CTL formulas if for all $\psi \in C$
 $s_i \models \psi$ for infinitely many i ($\text{G F } \psi$ in LTL)
- ▶ formulas in C are called **fairness constraints**
- ▶ A_C (E_C) denotes A (E) restricted to paths that are fair with respect to C

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Example



- ▶ path $1(376)^\omega$ is fair with respect to $\{I_B, P_B\}$ but not with respect to $\{I_A\}$
- ▶ $\mathcal{M}, 1 \not\models A_{\{R_B\}} F P_B$ because path $1(478)^\omega$ is fair with respect to R_B but $\mathcal{M}, i \not\models P_B$ for $i \in \{1, 4, 7, 8\}$

Lemma

$$\mathbf{E}_c[\varphi \mathbf{U} \psi] \equiv \mathbf{E}[\varphi \mathbf{U} (\psi \wedge \mathbf{E}_c \mathbf{G} \top)]$$

$$\mathbf{E}_c \mathbf{X} \varphi \equiv \mathbf{E} \mathbf{X} (\varphi \wedge \mathbf{E}_c \mathbf{G} \top)$$

New Algorithm (CTL Model Checking with Fairness Constraints)

required only for $\mathbf{E}_c \mathbf{G} \varphi$:

- ① restrict graph to states satisfying φ
- ② compute non-trivial strongly connected components (SCCs)
- ③ remove SCC S if there exists constraint $\psi \in C$ such that $s \not\models \psi$ for all states $s \in S$
- ④ label all states in resulting SCCs
- ⑤ compute and label all states that can reach labelled state in restricted graph computed in step ①

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Question

Which of the following statements hold for all models $\mathcal{M} = (S, \rightarrow, L)$ and states $s \in S$?

- A $\mathcal{M}, s \models \mathbf{E}_{\{p \wedge q\}} \mathbf{F}(q)$
- B $\mathcal{M}, s \not\models \mathbf{E}_{\{p\}} \mathbf{G}(\mathbf{E} \mathbf{F} p)$
- C $\mathcal{M}, s \models \mathbf{A}_{\{\neg q\}} \mathbf{F}(\mathbf{A} \mathbf{X} \neg q)$
- D $\mathcal{M}, s \models \mathbf{E}_{\{p\}} [\neg p \mathbf{U} p]$



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Theorem

satisfaction of LTL formulas in finite models is **decidable**

Two Approaches

- ① translate into CTL model checking with **fairness constraints**
- ② use **automata techniques**

Basic Strategy

$\mathcal{M}, s \models \varphi ?$

- construct **labelled Büchi automaton** $A_{\neg\varphi}$ for $\neg\varphi$
- combine $A_{\neg\varphi}$ and \mathcal{M} into single automaton $A_{\neg\varphi} \times \mathcal{M}$
- determine whether there exists accepting path in $A_{\neg\varphi} \times \mathcal{M}$



formula φ in LTL fragment with U and X as only temporal operators

Definition

closure $\mathcal{C}(\varphi)$ of φ consists of all subformulas of φ and their negations, identifying $\neg\neg\psi$ and ψ

Example

$$\mathcal{C}(a U (\neg a \wedge b)) = \{a, \neg a, b, \neg b, \neg a \wedge b, \neg(\neg a \wedge b), a U (\neg a \wedge b), \neg(a U (\neg a \wedge b))\}$$

- $\{a, b, \neg a \wedge b, a U (\neg a \wedge b)\}$ not elementary
- $\{a, b, a U (\neg a \wedge b)\}$ not elementary
- $\{a, b, \neg(\neg a \wedge b), a U (\neg a \wedge b)\}$ elementary
- $\{\neg a, \neg b, \neg(\neg a \wedge b), a U (\neg a \wedge b)\}$ not elementary
- $\{a, b, \neg(\neg a \wedge b), \neg(a U (\neg a \wedge b))\}$ elementary
- $\{a, \neg b, \neg(\neg a \wedge b), \neg(a U (\neg a \wedge b))\}$ elementary



Definition

set $B \subseteq \mathcal{C}(\varphi)$ is **elementary** if it is

- ① **consistent with respect to propositional logic:** for all $\varphi_1 \wedge \varphi_2 \in \mathcal{C}(\varphi)$ and $\psi \in \mathcal{C}(\varphi)$

- $\varphi_1 \wedge \varphi_2 \in B \iff \varphi_1 \in B \text{ and } \varphi_2 \in B$
- $\psi \in B \implies \neg\psi \notin B$
- $\top \in \mathcal{C}(\varphi) \implies \top \in B$

- ② **locally consistent with respect to U:** for all $\varphi_1 U \varphi_2 \in \mathcal{C}(\varphi)$

- $\varphi_2 \in B \implies \varphi_1 U \varphi_2 \in B$
- $\varphi_1 U \varphi_2 \in B \text{ and } \varphi_2 \notin B \implies \varphi_1 \in B$

- ③ **maximal:** for all $\psi \in \mathcal{C}(\varphi)$

- $\psi \notin B \implies \neg\psi \in B$



Definitions

- **states** of **automaton** A_φ are elementary subsets of $\mathcal{C}(\varphi)$
- **initial** states are those states containing φ
- **transition relation** Δ of A_φ : $(A, B) \in \Delta$ if and only if
 - ① for all $X\psi \in \mathcal{C}(\varphi) \quad X\psi \in A \iff \psi \in B$
 - ② for all $\varphi_1 U \varphi_2 \in \mathcal{C}(\varphi) \quad \varphi_1 U \varphi_2 \in A \iff \varphi_2 \in A \text{ or both } \varphi_1 \in A \text{ and } \varphi_1 U \varphi_2 \in B$
- **trace** is infinite sequence of valuations of propositional atoms
- trace t is **accepted** if there exists path π in A_φ such that
 - ① π starts in initial state of A_φ
 - ② π corresponds to trace t : $t_i = \{p \in \pi_i \mid p \text{ is atom}\}$ for all i
 - ③ π visits infinitely many states satisfying $\neg(\psi_1 U \psi_2) \vee \psi_2$, for every $\psi_1 U \psi_2 \in \mathcal{C}(\varphi)$



Example 1

$\varphi = Xa$

► $\mathcal{C}(\varphi) = \{a, \neg a, Xa, \neg Xa\}$

► states ① {a, Xa} ② {a, \neg Xa} ③ {\neg a, Xa} ④ {\neg a, \neg Xa}

► initial states ① ③

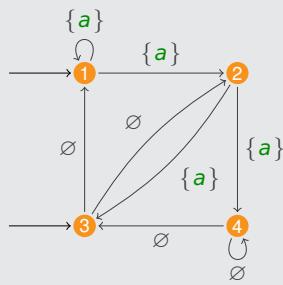
► transitions

	1	2	3	4
1	✓ ✓		{a}	
2		✓ ✓	{a}	
3	✓ ✓		∅	
4	✓ ✓		∅	

► trace $t_1 = \{a\}\{a\}\{a\}\emptyset^\omega$ is accepted: path ① ① ② ④ $^\omega$

► trace $t_2 = \emptyset\{a\}\emptyset\{a\}^\omega$ is accepted: path ③ ② ③ ① $^\omega$

► trace $t_3 = \{a\}\emptyset\emptyset\{a\}^\omega$ is not accepted



Example 2

$\varphi = aUb$

► $\mathcal{C}(\varphi) = \{a, \neg a, b, \neg b, aUb, \neg(aUb)\}$

► states ① {a, b, ϕ} ② {¬a, b, ϕ} ③ {a, ¬b, ϕ} ④ {a, ¬b, ¬ϕ} ⑤ {¬a, ¬b, ¬ϕ}

► initial states ① ② ③

► transitions

	1	2	3	4	5	
1	✓ ✓ ✓ ✓ ✓		{a, b}			
2	✓ ✓ ✓ ✓ ✓		{b}			
3	✓ ✓ ✓		{a}			
4		✓ ✓	{a}			
5	✓ ✓ ✓ ✓ ✓		∅			

► acceptance condition: paths cycling in state ③ are not accepting

► $\{a\}^\omega$ is rejected and $\{b\}\emptyset\{a\}^\omega$ is accepted

Basic Strategy

$\mathcal{M}, s \models \varphi$?

- construct labelled Büchi automaton $A_{\neg\varphi}$ for $\neg\varphi$
- combine $A_{\neg\varphi}$ and \mathcal{M} into single automaton $A_{\neg\varphi} \times \mathcal{M}$
- determine whether there exists accepting path in $A_{\neg\varphi} \times \mathcal{M}$

Theorem

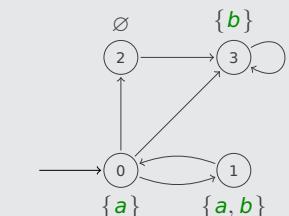
$\mathcal{M}, s \models \varphi \iff A_{\neg\varphi} \times \mathcal{M}$ has no accepting paths

Example

labelled Büchi automaton $A_{\neg\varphi}$ for $\varphi = aUb$

	1	2	3	4	5
{a, b, ϕ}	✓ ✓ ✓ ✓ ✓				
{¬a, b, ϕ}	✓ ✓ ✓ ✓ ✓				
{a, ¬b, ϕ}	✓ ✓ ✓				
→ {a, ¬b, ¬ϕ}			✓ ✓		
→ {¬a, ¬b, ¬ϕ}	✓ ✓ ✓ ✓ ✓				

model \mathcal{M}



acceptance condition: paths cycling in state ③ are not accepting

► product automaton $A_{\neg\varphi} \times \mathcal{M}$

→ 4 0 {	5 2 {	5 2 {
→ 5 0 ∅	2 3 {	2 3 {

► accepting path ④ 0 → ⑤ 2 → ② 3 → ⑤ 2 → ... $\Rightarrow \mathcal{M}, 0 \not\models \varphi$

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Huth and Ryan

- ▶ Section 3.2.5
- ▶ Section 3.4.5
- ▶ Section 3.6.2
- ▶ Section 3.6.3

Baier and Katoen

- ▶ Section 5.2 of **Principles of Model Checking** (MIT Press 2008)

Important Concepts

- | | | |
|---------------|------------------|----------------------------|
| ▶ A_C | ▶ E_C | ▶ fairness constraints |
| ▶ A_φ | ▶ elementary set | ▶ labelled Büchi automaton |
| ▶ adequacy | ▶ fair path | ▶ trace |
| ▶ closure | | |

homework for June 6

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First Exam on June 24

- ▶ registration in LFU:online is required before 23:59 on June 10
 - ▶ strict deadline: late email requests will be ignored
 - ▶ deregistration is possible until 23:59 on June 20
 - ▶ closed book
 - ▶ second exam on September 20, third exam on February 26, 2025

Preparation

- ▶ study previous exams
 - ▶ review homework exercises and solutions
 - ▶ study slides
 - ▶ visit Tutorium Wednesday, 16:15 – 17:00, SR 13
 - ▶ visit consultation hours AM Wednesday, 11:30 – 13:00, 3M07