





| Deductive Proofs | Reduction to Definitions | Proof by Contradiction | Inductive Proofs | Deductive Proofs | Reduction to Definitions | Proof by Contradiction | Inductive Proofs |
|---|--------------------------|--|------------------|--|--------------------------|------------------------------|------------------|
| Mutual Inductions (on Numbers) Image: the statements: A is off after n pushes iff n is even and A is is on after n pushes iff n is odd. are interdependent. Image: Mutual Induction to prove a group of statements $P_1(n), \ldots, P_k(n)$: • keep the statements separate • prove for all statements base and induction step separately. For on-off switch, we show • $P_1(n)$: The automata A is off after n pushes iff n is even. • $P_2(n)$: The automata A is on after n pushes iff n is odd. by using mutual induction. | | | | Deductive Proofs Reduction to Definitions Proof by Contradiction Inductive Proofs Base: we have to show (P₁(0); if), (P₁(0); only-if), (P₂(0); if), (P₂(0); only-if). case (P₁(0); only-if): we have to show: A is off after 0 pushes, if 0 is even. trivial. case (P₁(0); only-if): we have to show: A is off after 0 pushes, only-if 0 is even; that is A is off implies 0 is even, again trivial. Step: we have to show (P₁(n + 1); if), (P₁(n + 1); only-if), (P₂(n + 1); if), (P₂(n + 1); only-if). IH: P₁(n) and P₂(n). case (P₁(n + 1); only-if): we have to show: A off after (n + 1) pushes implies n + 1 is even. assumption: A is off after n + 1 pushes; hence A is on after n pushes, by IH: ((P₂(n); only-if), n is odd, hence n + 1 is even. | | | |
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| Deductive Proofs "If-then" and "if and only-if" Assertions Reduction to Definitions Proofs by Contradiction | | | | | | | |
| 5. Induc | tion on Numbers | | | | | | |
| 6. Structural Induction | | | | | | | |
| 7. Mutu | al Induction | | | | | | |
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