

Exercises.

7.0 Study Section 7.4–7.5.

7.1 Let \succsim denote a preorder that contains \sqsupset_{emb} for some WPO \sqsupset . Show that the strict part \succ of \succsim is well-founded.

7.2 Use Theorem 7.5.5. to prove termination of the TRS from Exercise 7.28 a).

7.3 Use Theorem 7.4.10 and/or 7.5.5 to prove termination of the TRS from Exercise 7.22.

7.4 Show termination of the following TRS:

$$\begin{aligned}(x^{-1})^{-1} &\rightarrow x \\(x + y)^{-1} &\rightarrow x^{-1} \times y^{-1} \\(x \times y)^{-1} &\rightarrow x^{-1} + y^{-1} \\x \times (y + z) &\rightarrow (x \times y) + (x \times z) \\(y + z) \times z &\rightarrow (x \times y) + (x \times z)\end{aligned}$$