

Functional Programming

WS 2007/08

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Overview

Week 2 - Lists

- Summary of Week 1

- List Basics

- List Functions

- Modules

Overview

Week 2 - Lists

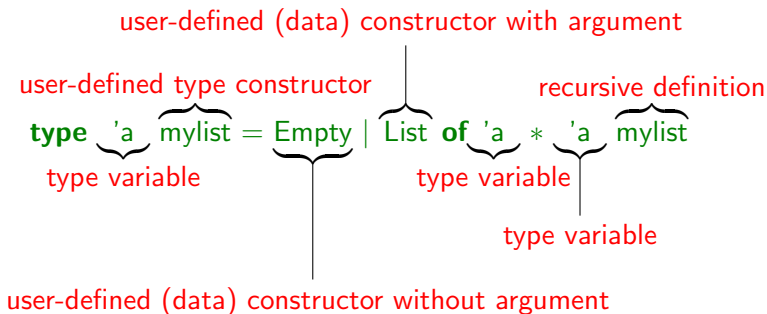
Summary of Week 1

List Basics

List Functions

Modules

User-defined Types



Recursion, Pattern Matching, and Currying

Recursion and Pattern Matching

```
let rec map (f, ls) = match ls with  
  | Empty -> Empty  
  | List (x, xs) -> List (f x, map (f, xs))
```

Currying

```
let rec map f ls = match ls with  
  | Empty -> Empty  
  | List (x, xs) -> List (f x, map f xs)
```

Syntactic Sugar

```
let rec map f = function  
  | Empty -> Empty  
  | List (x, xs) -> List (f x, map f xs)
```

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The Type of Lists

Polymorphic Lists

'[]' as syntactic sugar

`type 'a list = Nil | Cons 'a * 'a list`
 predefined type

infix '::' as syntactic sugar

Example

	type		type
<code>[true; false]</code>	bool list	<code>[(3, 2); (4, 3)]</code>	(int * int) list
<code>[1;3;5;7]</code>	int list	<code>[]</code>	'a list
<code>['a'; 'b'; 'c']</code>	char list	<code>1::2::3::[]</code>	int list
<code>["hello"; "world"]</code>	string list	<code>'a'::['b']</code>	char list

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Accessing List Elements - Selectors

```
let hd = function  
  | [] -> failwith "hd: empty list"  
  | x :: _ -> x  
;;
```

```
let tl = function  
  | [] -> failwith "tl: empty list"  
  | _ :: xs -> xs  
;;
```

A Polymorphic List Function

Example (Init)

```
let rec init i l = if l < 1 then [] else i :: init i (l - 1);;
```

- ▶ this function has type `'a -> int -> 'a list`
- ▶ hence it is polymorphic in `i`

```
init 'c' 2 → if 2 < 1 then [] else 'c' :: init 'c' (2 - 1)
           →+ 'c' :: init 'c' 1
           → 'c' :: if 1 < 1 then [] else 'c' :: init 'c' (1 - 1)
           →+ 'c' :: 'c' :: init 'c' 0
           → 'c' :: 'c' :: if 0 < 1 then [] else 'c' :: init 'c' (0 - 1)
           →+ ['c'; 'c']
```

Functions on Integer Lists

Example (Range, Sum, Prod)

```

let rec range m n =
  if m > n then
    []
  else
    m :: range (m + 1) n
;;
let rec sum = function
  | [] -> 0
  | x :: xs -> x + sum xs
;;
let rec prod = function
  | [] -> 1
  | x :: xs -> x * prod xs
;;
  
```

```

range 1 3 = [1; 2; 3]
range 3 2 = []
sum [1; 2; 3] = 1 + 2 + 3
sum [] = 0
prod [1; 2; 3] = 1 * 2 * 3
prod [] = 1
  
```

$$\text{sum (range 1 n)} = \sum_{i=1}^n i$$

Higher-Order Functions

- ▶ functions taking functions as arguments

Example (Map)

```
let rec map f = function
```

```
| [] -> []
```

```
| x :: xs -> f x :: map f xs
```

```
::
```

```
map succ [1; 2; 3] -> succ 1 :: map succ [2; 3]
                    -> 2 :: map succ [2; 3]
                    -> 2 :: succ 2 :: map succ [3]
                    -> 2 :: 3 :: map succ [3]
                    -> 2 :: 3 :: succ 3 :: map succ []
                    -> 2 :: 3 :: 4 :: map succ []
                    -> 2 :: 3 :: 4 :: [] = [2; 3; 4]
```

Fold - A Very Expressive Function

let rec fold f b = **function**

| [] -> b

| x :: xs -> f x (fold f b xs)

sum ls = fold (+) 0 ls

prod ls = fold (*) 1 ls

fold f b [e1; e2; ...; eN] = f e1 (f e2 (f e3 (... (f eN b) ...)))

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Structuring Code

Modules provide ...

- ▶ to split source code into several files
- ▶ separate namespaces for functions and types
- ▶ abstraction from concrete representations

Module Basics - Split Source Code

- ▶ for every module *Module* create **implementation** file *module.ml*
- ▶ code of each module goes into corresponding implementation file

Example

```
let hd = ...
let tl = ...
let rec init i l = ...
let rec map f = ...
let rec fold f b = ...
```

lst.ml

```
let rec range m n = ...
let sum = ...
let prod = ...
```

intLst.ml

Module Basics - Separate Namespaces

- ▶ refer to function *fun* from module *Module* by *Module.fun*
- ▶ no problem to have same function names in different modules

Example

Compute the greatest number that can be encoded in binary using n bits.

```
let pow2 n = IntLst.prod (Lst.init 2 n);;  
let maxbin n =  
  IntLst.sum (Lst.map pow2 (IntLst.range 0 (n - 1)))  
;;  
Format.printf "%i\n" (maxbin (read_int ()));;
```

maxbin.ml

Module Basics - Abstraction

- ▶ (optionally) create **interface** file `module.mli` for module `Module`
- ▶ **signature** (i.e., names and types) of module goes into corresponding interface file

Example

```

type 'a t
val empty : 'a t
val push : 'a -> 'a t -> 'a t
val pop : 'a t -> ('a * 'a t)
  
```

stck.mli

```

type 'a t = 'a list;;
let empty = [];;
let push e s = e :: s;;
let pop s = (Lst.hd s, Lst.tl s);;
  
```

stck.ml

```

type 'a t =
  | Empty
  | Full of 'a * 'a t
  ...
  
```

stck.ml