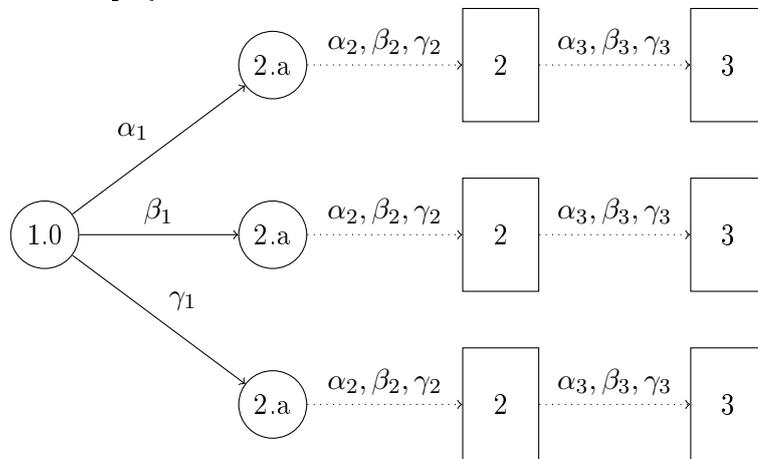
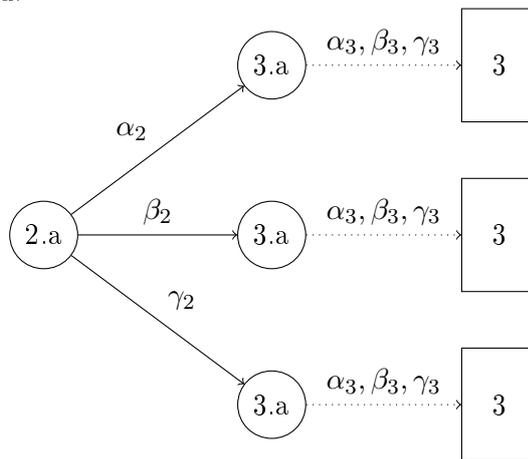


1. a) The decision maker prefers a lottery that gives the higher expected payoff in the worst possible state.  
 b) Monotonicity is violated.  
 c) Consider for example the following definition of  $f \succsim_T g$ :  $\sum_{s \in T} \min\{x \mid f(x|s) > 0\} \geq \sum_{s \in T} \min\{x \mid g(x|s) > 0\}$ . This would violate e.g. the strict subjective substitution axiom.
2. a) We write  $\alpha_i, \beta_i, \gamma_i$  for the strategies of players  $i = 1, 2, 3$ . To clarify the presentation, we first draw the first level completely, but compress the subgames for player 2 and player 3.



In place of the boxes for player 2 in the above picture, the following subgame has to substituted:



The important thing in this substitution is that information states for players 2 (and 3) need to be copied, as player 2 (player 3) don't know the decisions of the

other players. It is easy to see how to define the subgame that is substituted for the boxes for player 3 and the corresponding payoffs are computed: in case of an even vote, player 1 gets an additional decision node (e.g. marked 1.d) where she always chooses option  $\alpha$ , as this gives the best payoff for her.

- b) The algorithm on page 48 in the book transforms the above extensive game  $\Gamma^e$  into its normal representation  $\Gamma$ . The reduced strategic form is (in principal) obtained by removing randomly redundant strategies, but this doesn't change  $\Gamma$ . We render below one row of the strategic form of  $\Gamma$ , where we fix the votes of player 1 and 2 to  $\alpha$ .

$$\begin{array}{c} P_3 \\ \hline P_1 \quad \alpha_3 \quad \beta_3 \quad \gamma_3 \\ \hline \alpha_1 \quad (8,0,4) \quad (8,0,4) \quad (8,0,4) \end{array}$$

- c)  $\forall$  player  $i$ ,  $\forall$  nodes  $x$   $y$   $z$  controlled by  $i$   $\forall$  alternatives  $b$  at  $x$
- if  $y$  and  $z$  have the same information state and if  $y$  follows  $x$  and  $b$
  - $\exists$  node  $w$  and some alternative  $c$  at  $w$  such that  $z$  follows  $w$  and  $c$
  - $w$  is controlled by player  $i$ ,  $w$  has the same information label as  $x$  and  $c$  the same move label as  $b$

3. a) The game  $\Gamma_1$  has three Nash equilibria:

$$([C], [S]) \quad ([S], [C]) \quad \left( \frac{1}{101}[C] + \frac{100}{101}[S], \frac{1}{101}[C] + \frac{100}{101}[S] \right) .$$

- b) The only strongly dominated strategy in  $\Gamma_2$  is  $Pp$ , but note that  $Pp$  is *not* randomly redundant. Hence the fully reduced normal presentation of  $\Gamma_2$  equals  $\Gamma_2$ .
- c) The game  $\Gamma_2$  has a unique randomised Nash equilibrium:

$$\left( \frac{1}{3}[Rr] + \frac{2}{3}[Rp], \frac{2}{3}[M] + \frac{1}{3}[P] \right) .$$

4. Let  $([k], [j])$  for  $k \in M$ ,  $j \in N$  denote a pure equilibrium. Now, if we start the LH algorithm in vertex  $(\mathbf{0}, \mathbf{0})$ , we set the missing label to  $k$ . I.e., we traverse the unique edge that doesn't have label  $k$ . At the endpoint of this edge, we pick up a label that is the best response to strategy  $k$ , which is  $j$  by assumption. Moreover, as  $([k], [j])$  is an equilibrium, we know that  $k$  is also best response to  $j$ . I.e., if we drop  $j$  in the second polytope, we will pick up the best response to  $j$ , which happens to be  $k$ , the missing label.

<b>statement</b>	<b>yes</b>	<b>no</b>
To assert a player is <i>intelligent</i> , means the player makes decisions consistently in pursuit of her own objective.	<input type="checkbox"/>	<input checked="" type="checkbox"/>
Let $X$ be a finite set of decisions and $\Omega$ a finite set of states. For any decision $y \in X$ that is strongly dominated by a randomised strategy $\sigma \in \Delta(X)$ there exists a probability distribution $p \in \Delta(\Omega)$ such that $y$ is an optimal decision.	<input type="checkbox"/>	<input checked="" type="checkbox"/>
A set of vectors $S$ is convex if for any two vectors $p, q$ also $\lambda p + (1 - \lambda)q \in S$ , where $\lambda \in [0, 1]$ .	<input checked="" type="checkbox"/>	<input type="checkbox"/>
A game with incomplete information is a game in extensive form such that no two nodes have the same information set.	<input type="checkbox"/>	<input checked="" type="checkbox"/>
Given a finite game $\Gamma$ in strategic form, there exists at least one pure equilibrium.	<input type="checkbox"/>	<input checked="" type="checkbox"/>
5. In a Dutch auction the seller starts from a price of zero and continuously raises this price. The auction is over when the penultimate bidder leaves the auction and is won by the remaining bidder.	<input type="checkbox"/>	<input checked="" type="checkbox"/>
A game may have multiple equilibria, but at least one of the equilibria is efficient.	<input type="checkbox"/>	<input checked="" type="checkbox"/>
A two-person game is called nondegenerated if all randomised strategies $\sigma$ whose support has cardinality $k$ have at most $k$ pure best responses.	<input checked="" type="checkbox"/>	<input type="checkbox"/>
For a Nash equilibrium $(\sigma, \rho)$ of a nondegenerated two-person game, $\sigma$ and $\rho$ have support of equal size.	<input checked="" type="checkbox"/>	<input type="checkbox"/>
If we can show that $\text{NASH} \in \text{P}$ , then $\text{P} = \text{NP}$ follows.	<input type="checkbox"/>	<input checked="" type="checkbox"/>