Introduction to Scheduling

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What is Scheduling?

- Decision making process that deals with allocation of resources to tasks
 - o Processing units in a computing environment
 - o Routers (to handle packet traffic)
 - o Disk drives (I/O scheduling)
 - o Printers (print spooler)
 - o Embedded systems
 - 0 ..
- Goal is to optimise one or more objectives
- A **scheduling problem** can be described by a triplet (α, β, γ)
 - $\circ \ \alpha$ describes the resource environment
 - $\circ \,\, \beta$ describes the processing characteristics and constraints
 - $\circ \gamma$ describes the objective
 - o [Pinedo, Scheduling: Theory, Algorithms, and Systems, 1994]

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Resource Environments α

- Single machine
- Identical machines in parallel
- Machines in parallel with different speeds
- Unrelated machines in parallel
- Flow shop
- Flexible flow shop
- Job shop
- Flexible job shop
- Open shop

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Processing Characteristics and Constraints

β

- Release dates
- Preemptions
- Precedence constraints (worflows)
- Sequence dependent setup times (file transfers)
- Job families
- Batch processing
- Breakdowns
- Machine eligibility restrictions
- Permutation (FIFO in flow shops)
- Blocking (in flow shops)
- Nowait (in flow shops)
- Recirculation (in job shops)

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Objectives Functions γ

- Makespan (execution time)
- Turnaround (completion time)
- Response time
- Throughput
- Waiting time
- Communication time
- Load balance
- Processor utilisation
- Reliability
- Energy
- Economic cost

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Agenda

- Introduction
- Parallel and distributed applications
- Compiler construction
- Operating systems

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Agenda

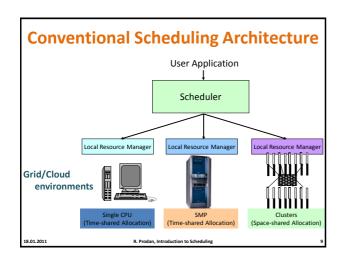
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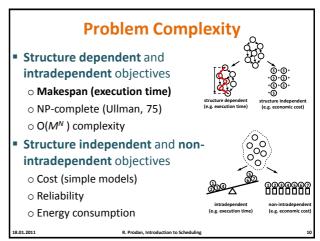
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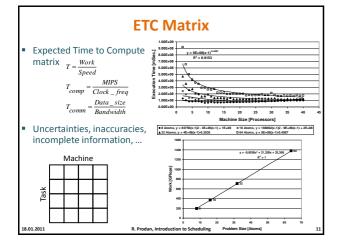
Scheduling Problem

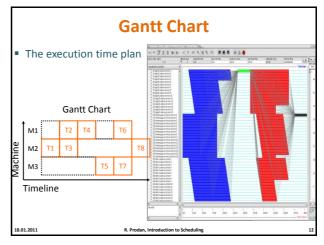
- Resource environment
 - o M unrelated machines in parallel
- Processing restrictions and constraints
 - N tasks
 - o Independent (parameter studies)
 - Workflow
- Objective function
 - o Execution time, ...
- Prediction matrix
 - o Objective function estimation for each task

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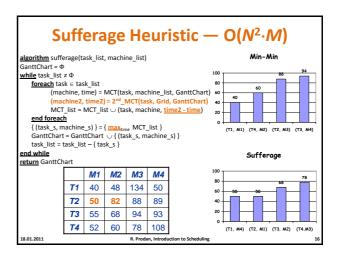
Independent Task Scheduling

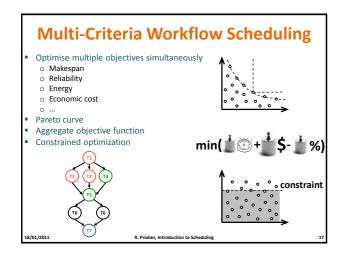
- O(N·M) heuristics
 - o Minimum Execution Time (MET)
 - o Minimum Completion Time (MCT)
 - o Switching Algorithm (SA)
 - o K-Percent Best (K-PB)
 - o Opportunistic Load Balancing (OLB)
- O(N²·M) heuristics
 - o Min-min
 - o Min-max
 - o Sufferage

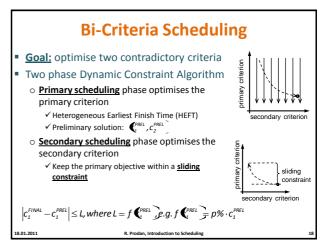
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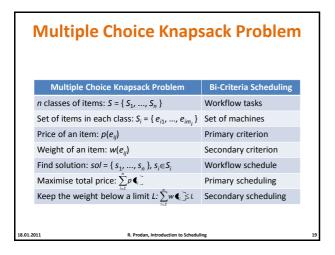
Min-Min Heuristic — $O(N^2 \cdot M)$ Determine the MCT for all the tasks Schedule only the task with the $\underline{\text{minimum}}$ $\underline{\text{MCT}}$ and reconsider the rest algorithm min-min(task_list, machine_list) GanttChart = Φ while task_list ≠ Φ $\underline{\textbf{foreach}} \; \mathsf{task} \in \mathsf{task_list}$ (machine, time) = MCT(task, machine_list, GanttChart) MCT_list = MCT_list ∪ (task, machine, time) $(task_s, machine_s) = min_{time} MCT_list$ GanttChart = GanttChart ∪ (task_s, machine_s) GanttChart = Gantt_ task_list = task_list = task_s M1 2 2 2 end while return GanttChart 2 M2 2 2 12

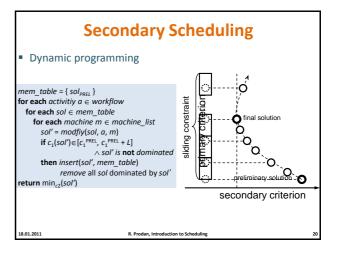
Min-Max Algorithm — $O(N^2 \cdot M)$ algorithm min-max(task_list, machine_list) GanttChart = Φ while task_list ≠ Φ $\underline{\text{foreach}}$ task \in task_list (machine, time) = MCT(task, machine_list, GanttChart) MCT_list = MCT_list ∪ (task, machine, time) end foreach (task_s, machine_s) = max_{time} MCT_list GanttChart = GanttChart ∪ (task_s, machine_s) task_list = task_list - task_s M1 2 2 2 2 end while return GanttChart M2 12 18.01.2011











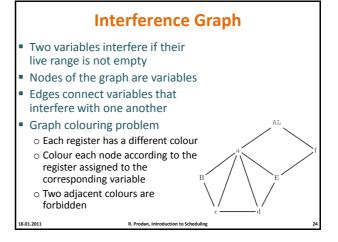
Game Theoretic Approach? Multiple schedulers representing end-user's objectives Maximise reliability Multiple resource managers representing resource provider's objectives Maximise income, throughput, utilisation, fairness Minimise energy consumption Single or multi-criteria objective for each participant Game theoretic negotiation Game theoretic negotiation Manager 1 Cloud Resource Manager 2 Cloud Provider 2 Manager 1 Cloud Provider 2 Manager 2 Cloud Provider 2 Manager 2 Cloud Provider 2 Manager 3 Cloud Provider 3 Manager 3 Manager 3 Cloud Provider 3 Manager 3 Manager 4 Manager 3 Manager 4 Manager 3 Manager 4 Manager 4 Manager 4 Manager 5 Manager 6 Manager 7 Manager 7 Manager 8 Manager 8 Manager 8 Manager 9 Manager 9

Agenda uted applications

- Introduction
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- Operating systems

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Register Allocation Map program variables to machine registers Build a control flow graph of basic program blocks Two types of variable references Use variables Define variables Program point between two consecutive instructions V is alive at program point p if There is a path from p to a use variable v V v is not redefined in between Live range = set of points where a variable is alive b: p₂, p₃, p₄, p₉ C : p₁, p₂, p₃, p₄, p₅, p₆, p₇, p₈, p₉, p₁₀, p₁₃, p₁₄, p₁₅



Interference Graph

Instructions Live vars b=a+2 c=b*b b=c+1 return b*a

Interference Graph

Instructions Live vars b = a + 2 c = b * b b = c + 1 b, a return b * a

Interference Graph

Instructions Live vars

b = a + 2

c = b * b

a,c

b = c + 1

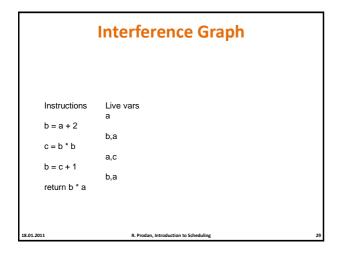
b,a

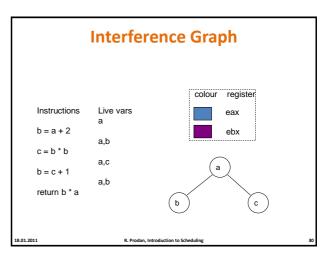
return b * a

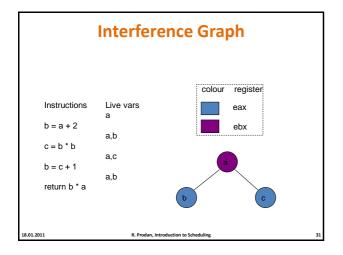
Interference Graph

Instructions Live vars

b = a + 2
b,a
c = b * b
a,c
b = c + 1
b,a
return b * a

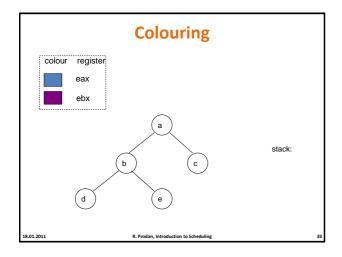


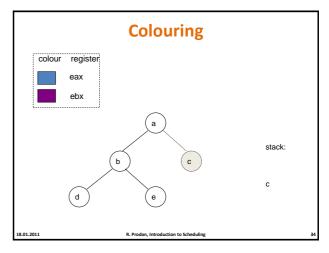


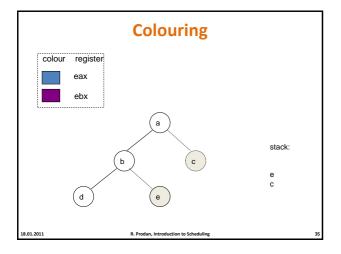


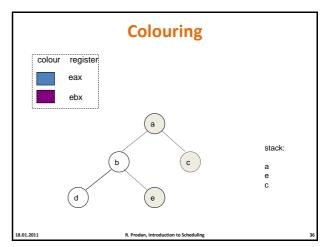
■ NP-complete problem ○ Fast and good heuristics required ■ Kempe's algorithm [1879] ■ Step 1: Simplify ○ Find a node with at most K-1 edges, remove it from the graph, push it onto a stack, and recurse ○ If the graph cannot be coloured, it will be simplified to graph in which every node has at least K neighbours (sometimes still K-colourable) ■ Step 2: Colour ○ After the simplified sub-graph has been coloured, add back the node on the top of the stack and assign it a colour not

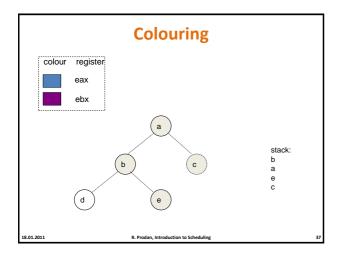
taken by the adjacent nodes

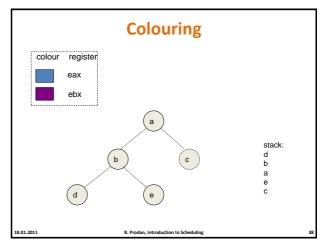


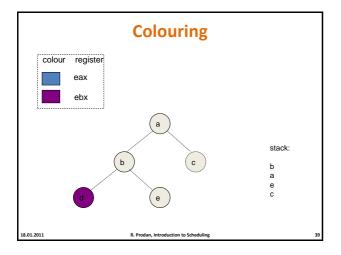


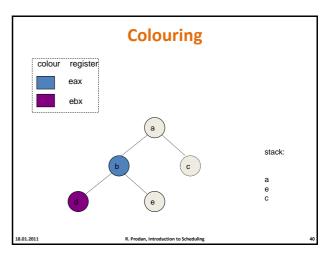


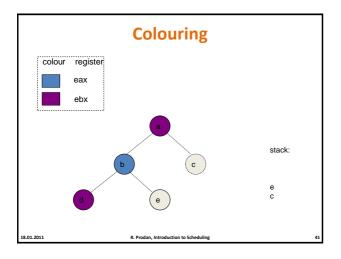


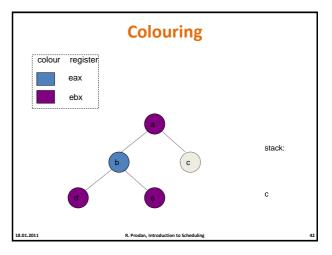


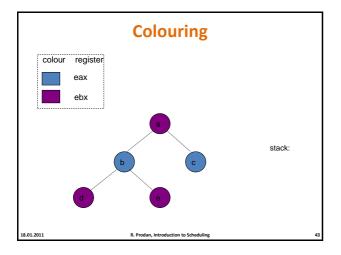


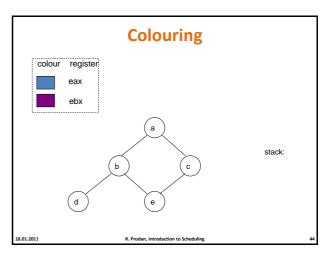


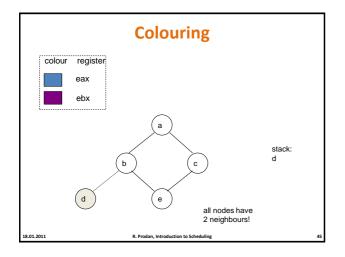


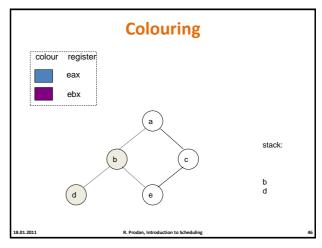


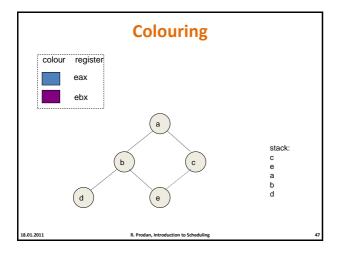


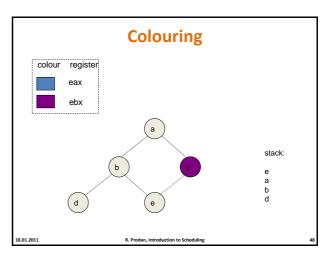


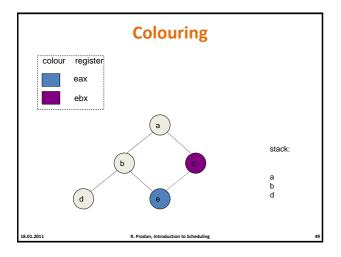


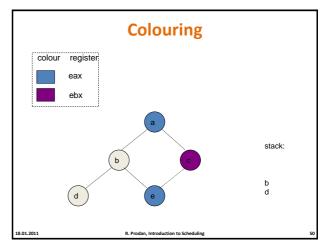


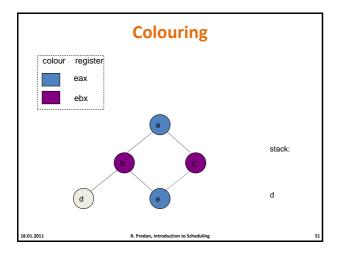


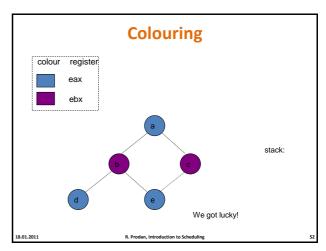


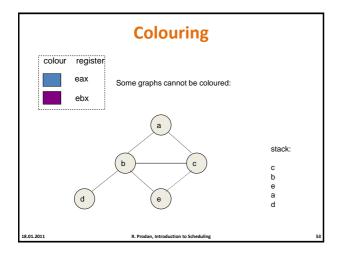


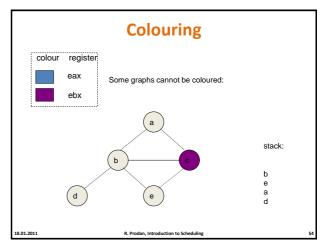


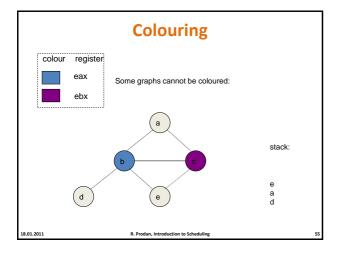


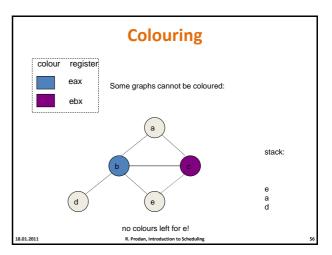












Chaitin's Algorithm

- Renumber
 - o Discover live range information in the source program
- Build
 - Build the interference graph.
- Coalesce
 - Merge the live ranges of non-interfering variables related by copy instructions (a:=b)
- Spill cost
 - o Compute the spill cost of each variable
- Simplify
 - o Kempe's colouring algorithm
- Spill Code
 - Insert loads and stores to commute values between registers and memory

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Operating Systems Scheduling

- Goal
 - $\,\circ\,$ Load balancing on shared memory systems (SMP and multi-core)
 - o Multiplex a single CPU for multiple processes
- Scheduling policy
 - o When it is time for a process to be removed from the CPU?
 - o Which ready process should be allocated to the CPU next?
- Enqueuer
 - $\,\circ\,$ Places a pointer to a process descriptor into the ready list
- Context switcher
 - $\circ\,$ Saves the contents of all processor registers for the process removed from the CPU in its process descriptor
- Dispatcher
 - o Selects one of the ready processes enqueued in the ready list and allocates the CPU

Preemptive versus Non-Preemptive Scheduling

- Non-preemptive scheduling
 - Process calls the yield() system call to release the CPU
 - Multiple processes could simultaneously yield to the scheduler
 - Scheduler selects and yields to one of the processes
- Preemptive scheduling
 - Interrupt system enforces periodic involuntary interruption of any process using an interval timer
 - o Invokes the scheduler and yield()
 - Each process gets to run in units of time slices (may be less than the interval time)

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yield(r, s) {
 memory[r] = PC;
 PC = memory[s];
}

 r and s are usually a function of the process's id

Simple Algorithms

Scheduling algorithm	CPU Utilization	Throughput	Turnaround time	Response time	Deadline handling	Starvation free
First In First Out	Low	Low	High	Low	No	Yes
Shortest Job First	Medium	High	Medium	Medium	No	No
Priority- based scheduling	Medium	Low	High	High	Yes	No
Round- robin scheduling	High	Medium	Medium	High	No	Yes
Multilevel queue scheduling	High	High	Medium	Medium	Low	Yes

Multiple Level Feedback Queue

- Linux 2.
- Minimise response and turnaround times without knowing the service time
- 140 priority queues
 - Static priorities 0—99 for real-time processes
 - o Static priorities 100—139 for normal processes set via nice system call
 - o Round-robin scheduling within each queue level
- O(1) insertion and selection time
 - A new process is positioned at the end of the top-level queue
 - Execute the process with the highest priority
- Dynamic priority calculation and adjustment
 - Preempt and move jobs at the end of next priority queue if they consume their time slice
 - o Move I/O blocking jobs to higher priority queues
- Drawbacks

■ Linux 2.6

queue to run

No cache awareness

- o CPU share not easy to calculate
- Possible to cheat the scheduler

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Shared Memory Multiprocessor

Scheduling

Each processor only selects processes from its own

Queues are periodically rebalanced (every 200 ms)

Separate run queue for each processor

Completely Fair Scheduler

- Linux 2.6.23
- One single run queue
- "wait runtime" value for each task
 - Time the task should run to become completely fair and balanced
 Always zero on "ideal" hardware
- Always run the task with the largest wait_runtime for its time slice
- Subtract the executed time slice from wait_runtime (minus the "fair share")
- Organise the tasks in a red-black tree based on their wait_runtime
 - O(log n) worst case search time



Processes with core affinity

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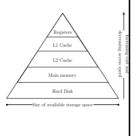
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Game Theoretic Scheduling?

- Different processes as game players with different resource requirements
 - o Thousands to millions
- Heterogeneous hardware
 - Hundreds of heterogeneous cores
 - Different latencies to memory modules
 - ✓On-chip shared memories
 - ✓ Distributed shared memory

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Conclusions

- Parallel and distributed applications
- Compilers
- Operating systems
- Starting point for some joint research?

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