Introduction to Model	Checking (VO)	WS 2010/2011 LVA	A 703503

 First name:

 Last name:

Matriculation number:

- Please answer all exercises in a readable and precise way.
- Please cross out solution attempts which are replaced by another solution.
- Please do not remove the staples of the exam.
- Cheating is not allowed. Everyone who is caught will fail the exam.

Exercise	Maximal points	Points
1	16	
2	21	
3	21	
4	12	
Σ	70	
Grade		

Exercise 1 (16 points)

We consider an extension of LTL with a yesterday operator Y where $Y \varphi$ should be true iff φ was true one time moment before. Moreover, at the beginning of the timeline, $Y \varphi$ is never true.

In the following example the semantics of Y is illustrated via a φ -expansion. Here, the truth values for a are determined by the input word.

time	0	1	2	3	4	5	6	7	8
а	1	0	0	1	0	0	1	1	
Υa	0	1	0	0	1	0	0	1	1

For each of the following formulas, provide an equivalent LTL formula without Y which accepts the same set of infinite words (without proof).

(i) $FYa \equiv$

(ii) YFa
$$\equiv$$

(iii) $G(Y a \Rightarrow b) \equiv$

 $(\mathrm{iv}) \ \mathsf{G} \, (\mathsf{a} \Rightarrow \mathsf{Y} \, \mathsf{b}) \equiv$

Exercise 2 (21 points)

Consider the following nanoPromela statement.

Construct the program graph for this statement. For the whole statement, additionally derive all transitions formally using the inference rules.

You may use abbreviations like "do ... od", "if ... fi", ...

Exercise 3 (5 + 16 points)

Consider the following formula:

$$\varphi = X (b U a) U (X a)$$

(i) Fill in all values of the φ -expansion for the given input word that can uniquely be determined where ... may be arbitrary.

а	0	1	0	0	1	$\begin{array}{c} 0 \\ 1 \end{array}$	0	0	0	
b	0	1	1	1	0	1	0	1	1	
bUa										
X (b U a) X a										
Xa										
φ										

(ii) Construct the automaton for φ . $\mathcal{A}_{\varphi} = (\{q_0\} \uplus 2^6, 2^2, q_0, \delta, F_1, F_2)$ where the Fischer Ladner closure is $cl(\varphi) = \mathsf{a}, \mathsf{b}, \underbrace{\mathsf{b} \, \mathsf{U} \, \mathsf{a}}_{\varphi_3}, \underbrace{\mathsf{X} (\mathsf{b} \, \mathsf{U} \, \mathsf{a})}_{\varphi_4}, \underbrace{\mathsf{X} \, \mathsf{a}}_{\varphi_5}, \varphi$

• $(c_1, \ldots, c_6)^T \in \delta(q_0, (d_1, d_2)^T)$ iff

•
$$(c_1, \ldots, c_6)^T \in \delta((b_1, \ldots, b_6)^T, (d_1, d_2)^T)$$
 iff

•
$$F_1 = \{(b_1, \dots, b_6)^T \mid$$

 $F_2 = \{(b_1, \dots, b_6)^T \mid$

Explicitly list all transitions leading to state $\boldsymbol{q} = (0,0,1,0,0,1)^T$.

Exercise 4 (12 points)

Each correct answer is worth 3 points. A wrong answer results in zero points (for that question, not for the whole exercise). Giving no answer is worth 1 point.

	Yes	No
Let \mathcal{A} be a GNBA with final state sets F_1, \ldots, F_k . Let \mathcal{B} be as \mathcal{A} where additionally for every i, j with $1 \leq i < j \leq k, F_i \cup F_j$ is added as new final state set to \mathcal{B} . Then $\mathcal{L}(\mathcal{A}) = \mathcal{L}(\mathcal{B})$.		
$\varphi U X \varphi \equiv \varphi \lor X \varphi$		
LTL model checking is PSPACE hard.		
In a channel system with a channel of capacity $c > 0$, sending and receiving is done simultaneously.		