

7. a)

$$\begin{aligned}
 q \vee \neg q &\approx \text{True} \\
 &\approx q \vee p \rightarrow \text{True} \\
 &\approx q \vee p \rightarrow (q \rightarrow p \rightarrow q)
 \end{aligned}$$

b)

- i) $\text{TV}(f) = \{(\text{T}, \text{F}), (\text{F}, \text{T}), (\text{F}, \text{F})\}$
- ii) $D = (\neg s_1 \wedge \neg s_2) \vee (s_1 \wedge \neg s_2) \vee (\neg s_1 \wedge s_2)$

8.

$$\frac{\frac{\frac{\frac{\frac{\frac{h(x) \approx x \in E}{E \vdash h(x) \approx x} \text{ (a)} \quad \frac{x \approx g(x) \in E}{E \vdash x \approx g(x)} \text{ (a)}}{(i, \sigma = \{x \mapsto a\})} \quad \frac{\frac{x \approx g(x) \in E}{E \vdash x \approx g(x)} \text{ (a)}}{(i, \sigma = \{x \mapsto a\})} \quad \frac{x \approx g(x) \in E}{E \vdash x \approx g(x)} \text{ (a)}}{(t)}}{(s)} \quad \frac{x \approx g(x) \in E}{E \vdash g(x) \approx x} \text{ (s)}}{(r)} \quad \frac{E \vdash g(x) \approx x}{E \vdash a \approx a} \text{ (k)} }{E \vdash h(a) \approx g(a)} \quad \frac{E \vdash h(a) \approx g(a)}{E \vdash f(h(a), g(x), a) \approx f(g(a), x, a)}$$

9. a) $G = (\{\text{S}, \text{B}\}, \{a, b\}, R, \text{S})$ mit den Regeln R :

$$\begin{aligned}
 S &\rightarrow aB \mid bS \mid \epsilon \\
 B &\rightarrow bB \mid aS
 \end{aligned}$$

b) $\underline{S} \Rightarrow a\underline{S} \Rightarrow ab\underline{S} \Rightarrow aba\underline{B} \Rightarrow aba\underline{B} \Rightarrow abab$

10. Lösung.

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// x1 := x1 ÷ x2
while x2 ≠ 0 do x1 := x1 - 1; x2 := x2 - 1 end;
// x3 := 0
while x3 ≠ 0 do x3 := x3 - 1 end;
// x3 ≠ 0 setzen falls x1 ≠ 0
while x1 ≠ 0 do x3 := x3 + 1 end

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□