

Automated Reasoning: Errata

Chapter “Propositional Logic”

- Page 8: The following sentences is no longer true as truth constants are now part of the language: “Note that the symbol \perp , representing contradiction, or falsity, is not part of our language of propositional logic.” Similar statements are made later in the context of resolution.
- Page 9, Definition of natural deduction: the rule for truth constant \top is missing.
- Page 11, Theorem 2.3: “propositional axioms” \rightarrow “propositional atoms”

Chapter “Syntax and Semantics of First-Order Logic”

- Page 15: The language contains also the truth constants \perp and \top .

Chapter “Soundness and Completeness of First-Order Logic”

- Page 24, Corollary 4.2. Change the definition of $c^{\mathcal{J}}$ as follows: “For any individual constant c , we set $c^{\mathcal{J}}$ such that $f(c^{\mathcal{J}}) = c^{\mathcal{I}}$ ”
- Page 32, Equation (4.2): “ Π_2 ” \rightarrow “ Π_1 ”.
- Page 36, extended the proof by the following paragraph: “In sum, there exists a collection of sets S admitting the satisfaction properties. Furthermore from the assumption that there exists no interpolation for the sentence $A \rightarrow C$, we conclude that $\{A, \neg C\} \in S$. Thus by model existence $\{A, \neg C\}$ is satisfiable. However then $A \rightarrow C$ cannot be valid. This shows the existence of an interpolant for $A \rightarrow C$.”

Chapter “Normal Forms and Herbrand’s Theorem”

- Page 46, the equivalence axioms E should read:

$$\forall x x \equiv x \wedge \forall x \forall y (x \equiv y \rightarrow y \equiv x) \wedge \forall x \forall y \forall z ((x \equiv y \wedge y \equiv z) \rightarrow x \equiv z) .$$

Chapter “Towards Automated Reasoning for First-Order Logic”

- Page 70. The definition of H_n should read as follows:

$$H_0 := \begin{cases} \{c \mid c \text{ is a constant in } \mathcal{L}\} & \exists \text{ constants in } \mathcal{L} \\ \{c\} & \text{otherwise} \end{cases}$$

$$H_{n+1} := \{f(t_1, \dots, t_k) \mid f^k \in \mathcal{L}, t_1, \dots, t_k \in H_n\}$$

- Page 71. The definition of the splitting rule should be as follows: “The rule consists in splitting \mathcal{C}' into $\mathcal{C}'_1 := \{A'_1, \dots, A'_n\} \cup \mathcal{D}$ and $\mathcal{C}'_2 := \{B'_1, \dots, B'_m\} \cup \mathcal{D}$, where A'_i is the result of deleting L from A_i and B'_j is the result of deleting $\neg L$ from B_j .”
- Page 87: adapt definition of NNF: “A formula is in NNF, if it does not contain implication, and every negation signs occur directly in front of an atomic formula.”
- Page 88: drop the indices in the condition “ $\forall x_1, \dots, \forall x_n <_A \exists y$ ”
- Page 89: Proof of Theorem 10.18: “ $E \wedge (\exists \vec{x}(E \wedge F) \rightarrow F\{\dots, x_i \rightarrow f_i(\vec{y}), \dots\}) \rightarrow$
“ $A \wedge (\exists \vec{x}(E \wedge F) \rightarrow F\{\dots, x_i \rightarrow f_i(\vec{y}), \dots\})$ ”
- Page 89: Add the following condition before the observation on splittings: “Suppose that each conjunction E_i contains at least one of the variables from \vec{x} .”

Automated Reasoning with Equality

- Page 99: “ $r \rightarrow_{\mathcal{R}} u \rightarrow t \rightarrow_{\mathcal{R}} u$; “ $s[u] \rightarrow_{\mathcal{R}} t \rightarrow s[u] = t$ ”
- Page 100: “the literal $L[t]\sigma'$ is maximal with respect to $D\sigma'$ ” \rightarrow “the literal $L[s']\sigma'$ is maximal with respect to $D\sigma'$ ”
- Page 102: “For the equality resolution rule: σ is a mgu of s and t , and $(s \neq t)\sigma$ is strictly maximal with respect to $C\sigma$.” \rightarrow “For the equality resolution rule: σ is a mgu of s and t , and $(s \neq t)\sigma$ is maximal with respect to $C\sigma$.”