Lastname:	 	 
Firstname:	 	 

Matriculation Number: \_\_\_\_\_

Exercise		Score
Modules and I/O		
Programming with Lists and Trees		
Programming with Abstract Datatypes and Functions		
Evaluation and Types		
Σ	90	

- You have 90 minutes to solve the exercises.
- The exam consists of 4 exercises, for a total of 90 points (so there is 1 point per minute).
- The available points per exercise are written in the margin.
- Don't remove the staple (Heftklammer) from the exam.
- Don't write your solution in red color.

## Exercise 1: Modules and I/O

Consider the following program. It asks the user for several numbers, which are then sorted and printed.

```
module MyProgram(main) where
 1
 2
 3 import qualified Data.List(sort)
 4
 5 \text{ main} :: IO ()
 6
   main = do
 7
      putStrLn "Welcome, please enter numbers to be sorted; end with the word "quit""
8
      run []
9
10 run :: [Integer] \rightarrow IO ()
    run xs = do
11
12
       x <- getLine
       if x == "quit"
13
14
          then finalize xs
15
          else run (x : xs)
16
17 finalize :: [Integer] \rightarrow IO ()
18 finalize xs = putStrLn (show (sort xs))
```

This program contains four mistakes that prevent it from being compilable by ghc.

- Identify these mistakes by providing line numbers,
- briefly explain the problem of each mistake, and
- explain how to correct the mistakes.

Note that all four errors are independent of one another.

(a) Mistake #1

(5)

(b) Mistake #2

(c) Mistake #3

(d) Mistake #4

(5)

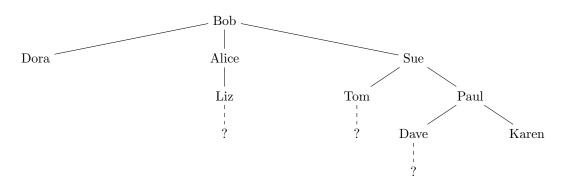
(5)

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#### Exercise 2: Programming with Lists and Trees

Suppose we have a collection of persons such that for each person we know his or her name and for some persons we also know the list of their children.

For example the following tree represents several persons, where the solid edges represent the is-child-ofrelation, and a dashed edge to a question mark indicates that we do not know the children of that person.



For instance, Bob has three children: Dora, Alice and Sue; Dora and Karen have no children; and for Liz, Tom and Dave it is not known how many children they have.

We model the trees by the following datatype definition:

```
data Tree = Node String (Maybe [Tree])
```

For the upcoming tasks you may use arbitrary Prelude functions. In particular concat :: [[a]] -> [a], map, and list comprehensions might be useful. You may use the functions defined in task (b) for later tasks, even if you did not solve task (b).

- (a) Define constants tom, karen, paul, sue :: Tree that correspond to the subtrees of the figure having (4) roots Tom, Karen, Paul and Sue, respectively.
- (b) Define two functions person :: Tree -> String and children :: Tree -> [Tree]. The former (4) returns the name at the root of a tree and the latter returns the direct subtrees. For instance, person sue = "Sue"; the expression children sue should evaluate to the same list as [tom, paul]; and both children tom and children karen result in the empty list.
- (c) Define a function grandChildren :: Tree -> [String] which computes a list of all known grandchildren (6) dren of the person at the root of the tree.
   For instance, grandChildren sue should result in ["Dave", "Karen"] since these are the only known grandchildren of Sue.
- (d) Define a function descendants :: Tree -> [String] which computes a list of all known descendant (8) of a specific person. For instance, descendants sue should result in a list which contains the names of Tom, Paul, Dave and Karen (in any order); and the descendants of the example tree above (with Bob as root) should be a list of all names of the figure except for "Bob" himself.
- (e) Define a function unknownGC :: Tree -> Bool which should return True if and only if the person at the root of the input tree might have unknown grandchildren. For instance, unknownGC sue evaluates to True, since we do not know the children of Tom. By contrast, unknownGC invoked on Bob should deliver False, since his grandchildren are exactly Liz, Tom and Paul.

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#### Exam 1 – A

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(3)

(3)

(6)

# Exercise 3: Programming with Abstract Datatypes and Functions

Consider an abstract datatype for sets, with the following signature:

empty :: Set a	the empty set
member :: Eq a => a -> Set a -> Bool	check whether element is in a set
insert :: Eq a => a -> Set a -> Set a	add an element to a set
complement :: Eq a => Set a -> Set a	compute the complement of a set

Here, the usual laws of mathematical sets should be satisfied, e.g.,

```
not (member x empty)
member x (insert x set)
x /= y ==> member x (insert y set) = member x set
member x (complement set) <==> not (member x set)
```

(a) Implement a function listToSet :: Eq a => [a] -> Set a. It converts a list of elements into an equivalent set of elements by using the functions of the abstract datatype.
 Example: member x (listToSet [1 9 3]) should be satisfied if and only if x is one of the numbers 1

Example: member x (listToSet [1,9,3]) should be satisfied if and only if x is one of the numbers 1, 9 or 3.

Next we consider an implementation of sets by functions. To be more precise, the functions encode whether an element is contained in a set or not.

data Set a = Fun (a -> Bool)

```
exampleSet :: Set Integer
exampleSet = Fun (<= 10) -- the set of all integers below 10</pre>
```

- (b) Implement empty.
- (c) Implement member.
- (d) Implement complement and insert.
- (e) Consider four further set operations: intersection of two sets; union of two sets; computing the cardinality (i.e., size) of a set; and removal of an element from a set. At least one of these set operations cannot be implemented with our representation. Which one? And why?

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#### **Exercise 4: Evaluation and Types**

In each multiple choice question, exactly one statement is correct. Marking the correct statement is worth 4 points, giving no answer counts 1 point, and marking multiple or a wrong statement results in 0 points.

Consider the following program.

foo  $[] = "{}"$ foo xs = "{" ++ foldr (\ x s -> show x ++ "," ++ s) "}" xs bar  $(0 : \_) [] = 1$ bar (x : y) = x(a) What is the most general type of foo? (4)□ foo :: [String] -> String  $\Box$  foo :: [a] -> String  $\Box$  foo :: Show a => [a] -> String  $\Box$  foo :: Show a => [a] -> [a] (b) What is the result of invoking take 7 \$ foo [1..]? (4) $\Box$  "{1,2,3,"  $\Box$  "{1,2,3,4,5,6,7,}"  $\Box$  "{1,2,3,4,5,6,7}"  $\Box$  the first character '{' is displayed and then the program does not terminate (c) What is the most general type of bar? (4)□ bar :: [a] -> [b] -> Int  $\Box$  bar :: (Eq a, Num a) => [a] -> [b] -> a  $\Box$  bar :: (Eq a, Num c) => [a] -> [b] -> c  $\Box$  bar :: (Eq a, Num a, Num c) => [a] -> [b] -> c (d) Consider the evaluation of the following expression w.r.t. Haskell's evaluation strategy. (4)bar (2 + 3 : [4] ++ [5]) ([6] ++ [7]) Choose the correct statement.  $\Box$  First [6] ++ [7] is evaluated, then the second bar-equation is applied, and finally 2 + 3 is evaluated.  $\Box$  First 2 + 3 is evaluated, and then the second bar-equation is applied.  $\Box$  First 2 + 3 is evaluated, then [4] ++ [5], then [6] ++ [7] and finally the second barequation is applied.  $\Box$  None of the above statements is correct. (e) Assume we enter the expression [(x, y) | x < - ["ab", "cde", "fgh"], y < length x, y < - [1..3]](4)in ghci. What will be the result? □ [("ab",1),("cde",1),("cde",2),("fgh",1),("fgh",2)] [("ab",1),("cde",1),("fgh",1),("cde",2),("fgh",2)] □ [("a",1),("c",1),("cd",2),("f",1),("fg",2)]

 $\Box$  We get a compile error, since the expression is not allowed in Haskell.