Lastname:			
Firstname:			
Matriculati	on Number		

Exercise	Points	Score
Modules and I/O	20	
Programming with Lists and Trees	30	
Programming with Abstract Datatypes and Functions	20	
Evaluation and Types	20	
Σ	90	

- You have 90 minutes to solve the exercises.
- The exam consists of 4 exercises, for a total of 90 points (so there is 1 point per minute).
- The available points per exercise are written in the margin.
- Don't remove the staple (Heftklammer) from the exam.
- Don't write your solution in red color.

Exercise 1: Modules and I/O

Consider the following program. It asks the user for several numbers, which are then sorted and printed.

```
module MyProgram(main) where
 1
 2
 3 import Data.List(sort)
 4
 5 main :: IO ()
 6 main = do
 7
     putStrLn "Welcome, please enter numbers to be sorted; end with the word \"quit\""
8
9
10 run :: [Integer] -> IO ()
   run xs = do
11
12
      x <- getLine
13
      if x == "quit"
14
         then finalize xs
15
         else run ((read x :: Integer) ++ xs)
16
17 finalize :: [Integer] -> IO ()
18 finalize xs = putStrLn (sort xs)
```

This program contains four mistakes that prevent it from being compilable by ghc.

- Identify these mistakes by providing line numbers,
- briefly explain the problem of each mistake, and
- explain how to correct the mistakes.

Note that all four errors are independent of one another.

(a) Mistake #1

(5)

(b) Mistake #2

(5)

(c) Mistake #3

(5)

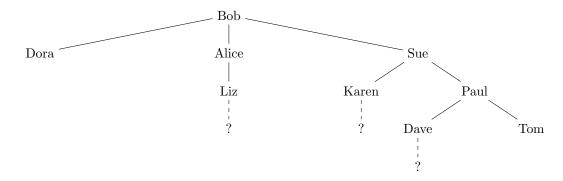
(d) Mistake #4

(5)

Exercise 2: Programming with Lists and Trees

Suppose we have a collection of persons such that for each person we know his or her name and for some persons we also know the list of their children.

For example the following tree represents several persons, where the solid edges represent the is-child-ofrelation, and a dashed edge to a question mark indicates that we do not know the children of that person.



For instance, Bob has three children: Dora, Alice and Sue; Dora and Tom have no children; and for Liz, Karen and Dave it is not known how many children they have.

We model the trees by the following datatype definition:

data Tree = Node String (Maybe [Tree])

For the upcoming tasks you may use arbitrary Prelude functions. In particular concat :: [[a]] -> [a], map, and list comprehensions might be useful. You may use the functions defined in task (b) for later tasks, even if you did not solve task (b).

- (a) Define constants tom, karen, paul, sue :: Tree that correspond to the subtrees of the figure having roots Tom, Karen, Paul and Sue, respectively.
- (b) Define two functions person :: Tree -> String and children :: Tree -> [Tree]. The former returns the name at the root of a tree and the latter returns the direct subtrees. For instance, person sue = "Sue"; the expression children sue should evaluate to the same list as [karen, paul]; and both children tom and children karen result in the empty list.
- (c) Define a function grandChildren :: Tree -> [String] which computes a list of all known grandchildren of the person at the root of the tree.
 For instance, grandChildren sue should result in ["Dave", "Tom"] since these are the only known grandchildren of Sue.
- (d) Define a function names:: Tree -> [String] that computes a list of all names that occur within a tree. For instance, names sue should be a list which contains the names of Sue, Karen, Paul, Dave and Tom (in any order); and names applied on the example tree above (with Bob as root) should result in a list of all names that occur the figure.
- (e) Define a function insertChildren :: String -> [Tree] -> Tree -> Tree with the following behavior. insertChildren name ch t computes a tree which is similar to t except that:
 - If name does not occur in t, then t is returned.
 - If name occurs in t, such that the children of name are unknown in t, then in the resulting tree name will have children ch.
 - If name already has a known list of children in t, an error should be raised.

For instance, insertChildren "Dave" [] sue will successfully replace the unknown children of Dave by the empty list of children, insertChildren "Marc" [] sue will be same tree as sue, and the invocation of insertChildren "Tom" [] sue will result in an error.

(4)

(4)

(7)

(9)

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(4)

(4)

Exercise 3: Programming with Abstract Datatypes and Functions

Consider an abstract datatype for sets, with the following signature:

empty :: Set a -- the empty set

member :: Eq a => a -> Set a -> Bool -- check whether element is in a set

insert :: Eq a => a -> Set a -> Set a -- add an element to a set

complement :: Eq a => Set a -> Set a -- compute the complement of a set

Here, the usual laws of mathematical sets should be satisfied, e.g.,

not (member x empty)

member x (insert x set)

x /= y ==> member x (insert y set) = member x set
member x (complement set) <==> not (member x set)

(a) Implement a function setOfList :: Eq a => [a] -> Set a. It converts a list of elements into an equivalent set of elements by using the functions of the abstract datatype.

Example: member x (setOfList [1,9,3]) should be satisfied if and only if x is one of the numbers 1, 9 or 3.

Next we consider an implementation of sets by functions. To be more precise, the functions encode whether an element is contained in a set or not.

data Set a = Fun (a -> Bool)

exampleSet :: Set Integer

exampleSet = Fun (<= 10) -- the set of all integers below 10

- (b) Implement empty. (3)
- (c) Implement member.
- (d) Implement complement and insert. (6)
- (e) Consider four further set operations: intersection of two sets; union of two sets; testing whether a set is empty; and removal of an element from a set. At least one of these set operations cannot be implemented with our representation. Which one? And why?

20

(4)

(4)

(4)

(4)

Exercise 4: Evaluation and Types

In each multiple choice question, exactly one statement is correct. Marking the correct statement is worth 4 points, giving no answer counts 1 point, and marking multiple or a wrong statement results in 0 points.

Consider the following program.

```
foo [] = "{}"
foo xs = "{" ++ foldr (\ x s -> show x ++ "," ++ s) "}" xs
bar (_ : []) [] = 1
bar (x : y) _ = x
```

(a) What is the most general type of foo?

☐ foo :: [String] -> String
☐ foo :: Show a => [a] -> [a]
☐ foo :: Show a => [a] -> String

☐ foo :: [a] -> String

(b) What is the result of invoking foo \$ take 7 [1..]?

□ "{1,2,3,"

 \square "{1,2,3,4,5,6,7,}"

 \square "{1,2,3,4,5,6,7}"

☐ the first character '{' is displayed and then the program does not terminate

(c) What is the most general type of bar?

□ bar :: [a] -> [b] -> Int

 \square bar :: (Num a) => [a] -> [b] -> a

 \square bar :: (Num c) => [a] -> [b] -> c

 \square bar :: (Num a, Num c) => [a] -> [b] -> c

(d) Consider the evaluation of the following expression w.r.t. Haskell's evaluation strategy.

Choose the correct statement.

☐ First 2 + 3 is evaluated, then [4] ++ [5] is evaluated, and finally the second bar-equation is applied.

□ First 2 + 3 is evaluated, then [4] ++ [5], then [6] ++ [7] and finally the second barequation is applied.

 \square First [4] ++ [5] is evaluated, then the second bar-equation is applied, and finally 2 + 3 is evaluated.

 \square None of the above statements is correct.

(e) Assume we enter the expression [(x, y) | x <- ["ab","cde","fgh"], y <- [1..3], y < length x] in ghci. What will be the result? (4)

 $\begin{tabular}{ll} \square & $[("ab",1),("cde",1),("fgh",1),("cde",2),("fgh",2)]$ \\ \end{tabular}$

☐ [("ab",1),("cde",1),("cde",2),("fgh",1),("fgh",2)]

 \square [("a",1),("c",1),("cd",2),("f",1),("fg",2)]

 \square We get a compile error, since the expression is not allowed in Haskell.