Lastname:				
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Exam 1

Version A

Exercise	Points	Score
Program Analysis Including Modules and I/O	20	
Programming with Lists	32	
Datatypes and Higher-Order Functions	26	
Evaluation and Types	12	
Σ	90	

- You have 90 minutes to solve the exercises.
- The exam consists of 4 exercises, for a total of 90 points (so there is 1 point per minute).
- The available points per exercise are written in the margin.
- Don't remove the staple (Heftklammer) from the exam.
- Don't write your solution in red color.
- Textual answers can be formulated in either English or German.

Exercise 1: Program Analysis Including Modules and I/O

Consider the following program. It chooses a random non-negative number and then asks the user to guess it.

```
1
   module Main(main, finalize) where
 2
 3
   import System.Random(randomIO) -- randomIO :: IO Integer
 4
 5 main = do
 6
     num <- randomIO
 7
     putStrLn "Try to guess my number"
     guessingGame (abs num) 1
 8
9
10 guessingGame :: Integer -> Integer -> IO String
11 guessingGame num n = do
12
     str <- getLine
13
     x <- (read str :: Integer)
14
     let reason = if x < num then "small" else "large"</pre>
15
     if x == num then finish n
16
     else do
17
       putStrLn $ "Your guess was too " ++ reason ++ ". Try again"
18
       guessingGame num n + 1
19
20 finish n = putStrLn $ "You guessed my number using " ++ show n ++ " tries"
```

This program contains four mistakes that cause compilation errors.

- Identify these mistakes by providing line numbers,
- briefly explain the problem of each mistake, and
- explain how to correct the mistakes.

Note that all four mistakes are independent of one another.

(a) Mistake #1 (5)

(b) Mistake #2

(5)

(c) Mistake #3

(5)

(d) Mistake #4

(5)

Exercise 2: Programming with Lists

Periodic functions can be represented by a list of initial values $vs = [v_1, ..., v_k]$ and a non-empty list of values $ws = [w_1, ..., w_m]$ that is repeated over and over again.

The function periodic :: [a] -> [a] -> Int -> a is then defined as follows: periodic vs ws n is the n-th element of the infinite list $[v_1, \ldots, v_k, w_1, \ldots, w_m, w_1, \ldots, w_m, w_1, \ldots, w_m, w_1, \ldots, w_m, \ldots]$ for every non-negative integer n. For example, if f = periodic [4,2] [5,1,3] then the results of evaluating f for arguments 0, ..., 8 are shown in the following table:

f O	1	1	1			1	1	1	
4	2	5	1	3	5	1	3	5	

Your task is to develop different (equivalent) implementations of periodic. You may freely use all Prelude functions. In particular, take, drop, splitAt, (!!), (++), filter, map and lookup might be useful.

- (a) Define a function infList for the infinite list described above, i.e., infList vs ws should evaluate to [v_1,...,v_k,w_1,...,w_m,w_1,...,w_m, ...], and provide the most general type of infList. Further define a function periodicInf as an implementation of periodic that is based on infList.
- (b) Define a function periodicN that implements periodic without constructing an infinite list and without using any predefined functions on lists (except for the list constructors). Evaluating periodicN vs ws n should require approximately n steps.
- (c) Define a function periodicFast :: [a] -> [a] -> Int -> a as an implementation of periodic. You should make use of the periodicity so that evaluating periodicFast vs ws n does not need many more than length vs + length ws steps, even if n is very large.

 Hint: Haskell contains functions div and mod to compute the quotient and the remainder of an integer division respectively.
- (d) Assume that a function g:: Int -> a is periodic, i.e. there exists a finite list vs and a non-empty finite list ws such that g = periodic vs ws. Assume also that the list vs ++ ws is distinct, i.e., it contains no duplicates.

Define a function getLists :: Eq a => (Int -> a) -> ([a], [a]) such that getLists g reconstructs vs and ws from g. In particular getLists (periodic vs ws) == (vs, ws) should be satisfied whenever vs and ws are two finite lists such that vs ++ ws is distinct and ws is non-empty.

Remark: you can get half of the points for this part if you instead implement an easier function getListSimple :: Eq a => (Int -> a) -> [a]. Here we assume that the input is a periodic function g = periodic [] ws and only ws is computed via getListSimple. In particular, the property getListSimple (periodic [] ws) == ws should be satisfied whenever ws is a finite, non-empty and distinct list.

(6)

(6)

(12)

26

(4)

Exercise 3: Datatypes and Higher-Order Functions

Consider the following program.

```
import Data.List(sort, sortOn)
-- sort :: Ord a => [a] -> [a]
-- sortOn :: Ord b => (a -> b) -> [a] -> [a]
-- sortOn f xs provides a sorted list ys of xs,
      such that f(ys !! (i - 1)) \le f(ys !! i) for all 1 \le i \le length ys;
-- sort and sortOn are closely related: sort = sortOn id
import Data.Char(toUpper)
-- toUpper :: Char -> Char
type Name = [String] -- a name might be composed, e.g., John Paul van de Boes
data Employee = Empl
 Name
  Int
 Float
           -- salary
nameOf (Empl name _ _) = name
mapEmp f g h (Empl name age salary) = Empl (f name) (g age) (h salary)
(a) Write down the most general types of nameOf and of mapEmp.
```

(b) Assume we want to write a function raiseSalary :: Employee -> Employee where the new salary is computed by the formula

```
new-salary = old-salary + age \times 10
```

Further assume our implementation uses the following structure.

```
raiseSalary = mapEmp undefined undefined
```

Either replace each undefined by a suitable λ -expression, or argue why raiseSalary cannot be implemented via mapEmp.

(c)	Assume we want to define a function toUpperEmployees :: [Employee] -> [Employee] that changes all names of all employees in a list so that they are written with uppercase letters. Choose a suitable implementation (4 points for the correct solution, 1 point for making no choice, 0 points for marking a wrong solution)	(4)
	☐ toUpperEmployees = toUpper	
	\square toUpperEmployees = map (mapEmp (map toUpper))	
	\square toUpperEmployees = map (mapEmp (map (map toUpper)) id id)	
	\square toUpperEmployees = map (mapEmp (map toUpper) id id)	
(d)	Assume we want to define a function sortedUppercaseNames :: [Employee] -> [Name] that returns a sorted list of the names of all employees in a list converted to uppercase. The sorting should also be done using the uppercase names. There are four different attempts to implement sortedUppercaseNames (sun for brevity).	(14)
	<pre>sun1 = map nameOf . sort . toUpperEmployees</pre>	
	<pre>sun2 = sort . toUpperEmployees . map nameOf</pre>	
	sun3 = map nameOf . sortOn nameOf . toUpperEmployees	
	<pre>sun4 = map nameOf . sortOn (nameOf . toUpperEmployees)</pre>	
	For each of the functions sun1, sun2, sun3 and sun4, indicate whether they are correct implementations	
	of sortedUppercaseNames or not; and for the incorrect ones, give a brief description of the problem.	

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Exercise 4: Evaluation and Types

n when using lazy evaluation.

In each multiple choice question, exactly one statement is correct. Marking the correct statement is worth 4 points, giving no answer counts 1 point, and marking multiple or a wrong statement results in 0 points.

Consider the following program.

foo n = bar 0 1 nbar x y n | n == 0 = x| otherwise = bar y (x + y) (n - 1)(a) What is the most general type of foo? (4) \square foo :: Int -> Int \square foo :: (Eq a, Num a) => a -> a \square foo :: (Eq a, Num a, Num b) => a -> b \square foo :: (Eq a, Num a, Eq b, Num b) => a -> b (b) What is the result of invoking foo n for some positive natural number n? (4) \Box 0 + 1 + 2 + ... + n \square n * n ☐ The n-th element of the list of Fibonacci numbers 0, 1, 1, 2, 3, 5, 8, 13, 21, ... \square None of the above (c) Assume that we evaluate foo n :: Int for some positive n :: Int. (4)Choose the correct statement. ☐ The memory consumption is constant for both innermost evaluation and lazy evaluation. ☐ The memory consumption grows linearly in n for both innermost evaluation and lazy evaluation. \square The memory consumption grows linearly in **n** when using innermost evaluation, but is constant when using lazy evaluation. ☐ The memory consumption is constant when using innermost evaluation, but grows linearly in