# universität innsbruck 

- Mark your completed exercises in the OLAT course of the PS.
- You can use a template .hs file that is provided on the proseminar page.
- Upload your modified .hs file in OLAT.
- Your .hs file must be compilable with ghci.


## Exercise 1 Programming with Pattern Matching and Recursion

In this exercise we will manipulate expressions in various ways. To this end we consider the datatype Expr of expressions of Lecture 2. We additionally represent variable assignments i.e., mappings from variables to numbers by type Assign.

```
data Expr = Variable String | Number Integer | Add Expr Expr | Negate Expr deriving Show
data Assign = Empty | Assign String Integer Assign deriving Show
```

For instance, exampleExpr represents $-(x+(-(y+3)))$, and exampleAssign corresponds to the assignment $\{x \mapsto 5, y \mapsto 12\}$ in the following code:
exampleExpr = Negate (Add (Variable "x") (Negate (Add (Variable "y") (Number 3))))
exampleAssign = Assign "x" 5 (Assign "y" 12 Empty)
For some of the following tasks the if-then-else function ite might be useful: given a Boolean and two arguments x and y of the same type, it selects one of the arguments depending on the truth value of the Boolean.
ite True $\mathrm{x} y=\mathrm{x}$
ite False x y = y

1. Define a function value : : String $\rightarrow$ Assign $\rightarrow$ Integer that returns the value of a variable in an assignment. If a variable does not occur in the assignment, you can you indicate an error via error "message" in Haskell. You may assume that assignments list each variable at most once.
(1 point)
For example, value "x" exampleAssign results in 5, and value "z" exampleAssign results in an error.
2. Define a function eval :: Assign -> Expr $\rightarrow$ Integer that evaluates an expression w.r.t. a given assignment. You may assume that all variables in the expression occur in the assignment, and that value is available, even if you did not solve the first task.
(1 point)
Example: eval exampleAssign exampleExpr results in $-(5+(-(12+3)))$, i.e., 10 .
3. Define a function containsVar : : String -> Assign -> Bool that determines whether a variable occurs in an assignment. (1 point)
Example: containsVar "x" exampleAssign results in True, whereas containsVar "z" exampleAssign results in False.
4. Define a function substitute : : Assign -> Expr $\rightarrow$ Expr that replaces all variables of the expression, that also occur in the assignment by the corresponding value. You may assume that both containsVar and value are available, even if you did not solve these tasks.
Example: substitute exampleAssign exampleExpr results in the Haskell encoding of $-(5+(-(12+3)))$, whereas the result of substitute (Assign "x" 7 Empty) exampleExpr represents $-(7+(-(y+3)))$.
5. We want to normalize expressions by moving negations inside the expression as far as possible. We say that an expression e is normalized if the negations only occur in front of variables or numbers. In Haskell this means that whenever Negate e1 is a subexpression of e, then e1 is of the form Variable x. Note that if e1 represents a number, then one can eliminate the Negate constructor by just negating the number.
Define a function normalize : : Expr $\rightarrow$ Expr that computes a normalized expression.
Example: normalize exampleExpr results in the Haskell encoding of $-x+(y+3)$.
