- Mark your completed exercises in the OLAT course of the PS.
- You can use a template .hs file that is provided on the proseminar page.
- Upload your modified .hs file in OLAT.
- Your .hs file must be compilable with ghci.

Exercise 1 Polymorphism and Trees
In this exercise we will consider a type for representing binary trees. To this end we consider the datatype Tree defined as

```
data Tree a = Node a (Tree a) (Tree a) | Leaf a
```

For instance, exampleTree represents the following tree:

exampleTree $=$ Node 1 (Leaf 2) (Node 3 (Node 4 (Leaf 5) (Leaf 6)) (Leaf 7))

1. Write a function height :: Tree a -> Integer that calculates the height of a binary tree. The height is the number of edges on the longest path between the root and a leaf.
(1 point)

Examples:
height (Leaf 'a') == 0
height exampleTree $==3$
2. Write a function flatten : : Tree a -> [a] which takes a tree as an argument and returns a list containing exactly the elements in the tree from left to right. In particular, each node element should appear in the list after the elements in its left subtree and before the elements in its right subtree.
(1 point)
Hint: (++) :: [a] -> [a] -> [a] is Haskell's predefined append-function for lists.
Examples:
flatten (Node 1 (Leaf 2) (Leaf 2)) == [2,1,2]
flatten exampleTree $==[2,1,5,4,6,3,7]$
3. A binary tree $t$ is said to be a binary search tree if flatten $t$ is a list whose elements appear in strictly increasing order. Write a function isSearchTree:: Ord a $\Rightarrow$ Tree a $\rightarrow$ Bool that takes a tree as an argument and returns True if and only if the tree is a binary search tree.
Hint: you may assume that flatten is available even if you did not solve question 2. It might be useful to define an auxiliary function isStrictlySorted : : Ord a => [a] -> Bool to determine whether the elements in a list are strictly increasing.
```
Examples:
isSearchTree (Leaf "hello") == True
isSearchTree exampleTree == False
isSearchTree (Node 3 (Leaf 1) (Node 6 (Leaf 4) (Leaf 11))) == True
```

4. Write a function elemDepth :: Eq a $\Rightarrow>$ a $\rightarrow$ Tree a $->$ Maybe Integer which determines whether an element is in a tree. If the element is in the tree and $d$ is the minimum depth at which the element appears, then Just d should be returned. Otherwise, Nothing should be returned.
Is the restriction Eq a necessary?
Hint: it might be useful to define an auxiliary function of type Maybe a -> Maybe a -> Maybe a to process results from recursive calls of elemDepth (see also slide 04/20).
The Haskell function min : : Ord a $=>$ a $->$ a $->$ a might also be useful.
Examples:
elemDepth 7 exampleTree == Just 2
elemDepth 15 exampleTree == Nothing
elemDepth 'b' (Node 'a' (Leaf 'b') (Node 'c' (Leaf 'b') (Leaf 'd'))) == Just 1
