

Automata and Logic

WS 2024/2025

LVA 703026 + 703027

Week 1

October 11, 2024

Solved exercises must be marked and solutions (as a single PDF file) uploaded in OLAT. The (strict) deadline is 7 am on October 11.

Exercises

- $\langle 2 \rangle$ 1. Design DFAs for the following sets.
 - (a) The set of strings in $\{a, b, c\}^*$ containing the substring *abc*.
 - (b) The set of strings $x \in \{a, b\}^*$ such that #a(x) is odd and #b(x) is a multiple of three.
- $\langle 2 \rangle$ 2. Let $M = (Q, \Sigma, \delta, s, F)$ be an arbitrary DFA. Prove by induction on |y| that

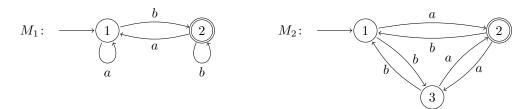
 $\widehat{\delta}(q, xy) = \widehat{\delta}(\widehat{\delta}(q, x), y)$

for all strings $x, y \in \Sigma^*$ and states $q \in Q$.

- (3) 3. Prove that the set $\{x \in \{0, 1, 2\}^* \mid x \text{ is a ternary representation of a multiple of four}\}$ is regular.
- $\langle 3 \rangle$ 4. (a) Prove that regular sets are effectively closed under set difference (-) defined as:

$$A - B = \{ x \mid x \in A \text{ and } x \notin B \}$$

(b) Consider the DFAs



Construct a DFA M such that $L(M) = L(M_1) - L(M_2)$.