



Advanced Functional Programming

Week 8 - Backtracking during Parsing, Applicative Functors, Monad Transformers

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Details on Backtracking during Parsing

Last Week

- context free grammars
- parser combinators, example: Parsec library
 - several primitives to read a single char, e.g., char, anyOf, noneOf, space, satisfy, eof
 - combinators to combine parsers, e.g., many, many1, sepBy, endBy
 - p1 <|> p2 and try p1 are used for non-determinism and back-tracking
 - if p1 succeeds (Ok), then p1 <|> p2 and try p1 succeed
 - if p1 fails after consuming some input (F+), then p1 <|> p2 fails (F+)
 - if p1 fails without consuming input (F0), then p1 <|> p2 switches to p2
 - if p1 fails (F+ or F0) then try p1 fails with F0

(backtrack to position in input stream, when p1 was started)

- p1 <|> p2 tries p2 only if p1 fails with F0
- try p1 <|> p2 tries p2 only if p1 fails

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funapp = do

Simple ARI Parser (Demo08_Parser_ARI_Do_Blocks)

```
charS '('
lexeme p = do
                                                  f <- identifier</pre>
  a <- p
  spaces
                                                  ts <- many term
 return a
                                                  charS ')'
                                                  return $ Fun f ts
identChar = noneOf " \t\n();:"
identifier = lexeme $ many1 identChar
                                                 rule = do
                                                    try $ do
                                                      charS '('
term = variable <|> funapp
                                                       exactlyS "rule"
variable = do
                                                   1 <- term
 i <- identifier
                                                    r <- term
 return $ Var i
                                                    charS ')'
                                                   return (1,r)
charS c = do
  _ <- lexeme (char c)</pre>
                                                 exactlyS s = lexeme $ try $ do
 return ()
                                                   _ <- string s</pre>
                                                  notFollowedBy identChar <?> "..." ++ s
```

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Explanations

- lexeme
 - lexeme p has the same behavior as p, except that trailing white space is removed
 - invariant: all parsers remove trailing white space
 - advantage: later parsers can always assume that there is no leading white space
 - only exception: the main parser has to once remove leading white space
- charS is just a version of char that strips trailing white space and does not return the resulting character
- in the rule parser, try is used to backtrack to the beginning, if the initial part is not of shape ("rule where rule cannot be extended into a longer identifier
- to ensure the latter we use exactlyS, which basically is using string "rule" followed by the combinator notFollowedBy; this combinator usage enforces that no identifier character is present after "rule"
 - "rule a" is accepted by exactlyS "rule", and one jumps to the beginning of "a"
 - "rules a" is not accepted by exactlyS "rule", and one jumps back to the beginning of the text, complaining about "...rule"

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Example: Small Try-Blocks in ARI Parser

• have a look at the rule parser again

```
rule = do
    try $ do
        charS '('
        exactlyS "rule"
    l <- term
    r <- term
    charS ')'
    return (l,r)</pre>
```

- try is closed after keyword "rule" has been detected
 - hence, after reading (rule the applied parser is fixed
- one can define similar parsers p1, ..., pn, for each function symbol in a TRS
 - hence, choice [p1,...,pn] will quickly select the correct parser for (fNameI t1 ... tk), namely after reading (fNameI_□, without major backtracking

When to Use Try

- with try and <|> one can easily write inefficient parsers
- try gives rise to backtracking, and this can become expensive

```
• example: detect cases of (ab)^* \cup \{a,b\}^*c pQuadratic = try (string "ab" >> pQuadratic) <|> (eof >> return "(ab)^*") <|> (many (oneOf "ab") >> string "c" >> eof >> return "end in c")
```

- solution: close try-blocks, as soon as the applicable rule has been determined
- reason for linear time is the behavior of <|>
 - whenever p1 in p1 <|> p2 consumes at least one character, then p2 is not tried
 - consequently, if input starts with "ab", then other alternatives are not tried in pLinear

Applicative Functors

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Applicative Functors, Applicative Style

- have a look at an excerpt of a previous parser
 parse1 = many (oneOf "ab") >> string "c" >> return "end in c"
- here, >> is used do write the parser more succinctly
- alternative without >>

```
parse2 = do
   _ <- many (oneOf "ab")
   _ <- string "c"
   _ <- eof
   return "end in c"</pre>
```

- observation: we often invoke several parsers, but only some of them contribute to the parsed result
- >> is only one possible way to combine results: throw away result of left parser
- aim: more flexible combinations
- solution: use applicative functors and applicative style

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Applicative Functors: Laws

```
laws
```

```
    pure id <*> v = v (identity)
    pure g <*> pure x = pure (g x) (homomorphism)
    pure (.) <*> u <*> v <*> w = u <*> (v <*> w) (composition)
    u <*> pure y = pure ($ y) <*> u (interchange)
```

- consequence: fmap g x = pure g <*> x
 so fmap can be implemented via pure and <*>
- note the similarity and difference of type of fmap, <\$> and <*>
 (<\$>), fmap :: (a -> b) -> f a -> f b
 (<*>) :: f (a -> b) -> f a -> f b
- as we have seen, this small change is sufficient to allow arbitrary liftings of *n*-ary functions into the applicative functor

Applicative Functors, Difference to Functors

- known: monads have more structure than functors
- applicative functors are between monads and functors

```
class Functor f => Applicative f where
  (<*>) :: f (a -> b) -> f a -> f b
  pure :: a -> f a
```

 applicative functors are stronger than Functors: it is possible to lift n-ary functions to a sequence of n elements of an applicative functor, which is not possible with ordinary functors

```
n = 2
liftA2 :: Applicative f => (a -> b -> c) -> f a -> f b -> f c
liftA2 g x y = (pure g <*> x) <*> y

note the partial application: pure g <*> x :: f (b -> c)
since <*> associates to the left, one just writes pure g <*> x <*> y
arbitrary n: pure g <*> x1 <*> x2 <*> ... <*> xn
```

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Towards Programming in Applicative Style

- we have already seen that sequences of <*> can combine results
- sometimes it is helpful to disregard some of the results, while still having the effect of the functor
- therefore, there are several combinators, all with fixity declaration infix1 4
- in general, operators with a one sided arrow symbol > use only the result from that side

```
all types with * assume Applicative f, all with $ assume Functor f
(**) :: f (a -> b) -> f a -> f b
(**) :: f a -> f b -> f a
(*>) :: f a -> f b -> f b
($>) :: (a -> b) -> f a -> f b
($$) :: a -> f b -> f a
```

• example implementations

```
(<$) = fmap . const
u (*>) v = (id <$ u) <*> v
```

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Programming in Applicative Style

- combine the combinators of previous slide for more succinct code
- once one gets familiar with these, this does not hinder readability
- example: live demo to switch from Demo08_Parser_ARI_Do_Blocks to Demo08_Parser_ARI_Applicative
- example explanation of function application parser:

```
funapp = Fun <$> (charS '(' *> identifier) <*> many term <* charS ')'
```

- charS '(' *> identifier consumes (fName
 - since we are not interested in the open parenthesis, the result of the left parser is ignored by *>
 - result of parser will be just fName
- Fun <\$> (charS '(' *> identifier)
 - parsing is identical, but result will now be Fun fName, a partially applied constructor
- Fun <\$> (charS '(' *> identifier) <*> many term
 - additionally, many terms ts are parsed and result will be the term Fun fName ts
- Fun <\$> (charS '(' *> identifier) <*> many term <* charS ')'
 - a closing parenthesis is parsed, but this has no impact on the result, since <* looks to the left

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Applicative Functors and Monads (Continued)

- sometimes monad laws are too restrictive, if one just wants to have an applicative functor
- example: collect errors during computations
- monad laws enforce the following implementation of >>=, so that an error in the second argument of >> is ignored, if first argument results in error

```
instance Monad (Either e) where
  return = Right
  Left e >>= _ = Left e -- Left e1 >> _ = Left e1
  Right x >>= f = f x
```

• just requiring an applicative functor permits an implementation that collects errors

Applicative Functors and Monads

```
every Monad is an applicative functor
class Functor f => Applicative f where
pure :: a -> f a
  (<*>) :: f (a -> b) -> f a -> f b
  (*>) :: f a -> f b -> f b
class Applicative m => Monad m where
  (>>=) :: m a -> (a -> m b) -> m b
return = pure
```

monads are stronger than applicative functors

```
• (*>) = (>>), a1 <*> a2 = a1 >>= (\ f -> a2 >>= (\ x -> return (f x)))
```

- ullet consider a computation involving n (monadic or functor) values
 - for applicative functors, the computation of f <\$> v1 <*> v2 <*> ... <*> vn is possible, but each vi is computed independently, i.e., vi may not look into the results of v1,...,vi-1
 - this is in contrast to monads, where this is possible:

```
do { x1 <- v1; x2 <- v2 x1; ... xn <- vn x1 ... (xn - 1);
    return $ f x1 ... xn }</pre>
```

• example where monads are required: parser for terms can depend on parsed signature

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Monad Transformer

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Using Several Monads at Once: Monad Transformer

- sometimes, we would like to have the capabilities of several monads at once
- examples
 - use several states; solution: combine all states into one record datatype
 - use writer and state; solution: use RWS monad
 - use state and error; solution: write dedicated monad (PGM parser monad)
- last example is tedious
- better solution: use monad transformer
 - monad transformer takes a monad as input, and then adds another effect
 - example: take Maybe as input monad, and then add capabilities of State on top of it
 - monad transformers are all indicated by suffix T
 - newtype StateT s m a = ...
 this is the monad transformer to add State features
 - type State s = StateT s Identity
 the State monad is just the StateT monad transformer where one plugs in the Identity
 monad
 - newtype Identity a = Identity { runIdentity :: a } is the trivial monad
- most monads that have been presented are part of MTL, the monad transformer library

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Review Definition of Known Monads Again

• most monads are actually defined via their corresponding monad transformers

```
    data ParsecT s u m a = ...
type Parsec s u = ParsecT s u Identity
    newtype RWST r w s m a = ...
type RWS r w s = RWST r w s Identity
    newtype StateT s m a = ...
type State s = StateT s Identity
```

- ...; notable exception: for IO there is no IOT monad transformer
- with monad transformers we can easily combine multiple effects
 - RWST r w s Maybe combines RWS with Maybe error monad
 - RWST r w s IO combines RWS with IO monad
 - StateT st (ParsecT s u m) is monad transformer that adds State and Parsec features
 - Identity can always be used to terminate a stack of monad transformers, e.g.,
 MT1 s (MT2 r (... MTn u Identity))
- because of mentioned restriction, IO must always be at the inside

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Example: Just using IO Monad

• write function to list all subdirectories with number of entries per directory

Example: Collect Output in Writer Monad via WriterT

```
countEntries2Main :: FilePath -> WriterT [(FilePath, Int)] IO ()
countEntries2Main path = do
    contents <- liftIO . listDirectory $ path
    tell [(path, length contents)]
    flip mapM_ contents $ \name -> do
        let newName = path </>        name
        isDir <- liftIO . doesDirectoryExist $ newName
        when isDir $ countEntries2Main newName

countEntries2 :: FilePath -> IO [(FilePath, Int)]
countEntries2 = fmap snd . runWriterT . countEntries2Main
```

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Explanations

```
• countEntriesMain :: ... -> WriterT [(FilePath, Int)] IO ()
        • since the outer type is WriterT, the result type is an instance of MonadWriter [...]
        • therefore, tell :: [...] -> WriterT [...] m () is available
    • lift10 :: Monad10 m => 10 a -> m a lifts IO-actions to a corresponding monad
        • IO is a trivial instance of MonadIO where liftIO = id
        • there also is an instance (Monoid w, MonadIO m) => MonadIO (WriterT w m);
          this tells us that being an MonadIO instance is preserved by WriterT w
    • when :: Applicative f => Bool -> f () -> f () is if-then without else:
      when p s = if p then s else pure ()
    • runWriterT :: WriterT w m a -> m (a, w)
        • run the WriterT monad transformer
        • result will be in original monad m
        • output of writer will be made available in second component of result
        • similar to runWriter :: Writer w a -> (a, w)
    • overall: availability of both MonadWriter and IO;
      run runWriterT to convert WriterT w m a into m (a,w), i.e., eliminate WriterT
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```

Example for Stacking Monad Transformers

- example is an extension of the directory count example
 - extension 1: user must specify maximal recursion depth
 - extension 2: compute reached maximal recursion depth
- utilized monads
 - MonadIO is required for directory access
 - access via liftIO :: MonadIO m => IO a -> m a
 - use MonadReader to pass configuration around; that configuration stores recursion limit
 - access via ask :: MonadReader r m => m r
 - use MonadState to store the maximally reached recursion depth
 - access via get :: MonadState s m => m s and put :: MonadState s m => s -> m ()

Design of MTL

```
    several abstract classes, e.g., MonadWriter, MonadReader, MonadState, MonadIO,...
    several monad transformers, e.g., WriterT, ReaderT, StateT, ...
    n × n instance declarations
    (Monoid w, Monad m) => MonadWriter w (WriterT w m)
    MonadWriter instance
```

```
(Monoid w, Monad m) => MonadWriter w (writer w m)
(Monoid w, MonadIO m) => MonadIO (WriterT w m)
(Monoid w, MonadState s m) => MonadState s (WriterT w m) preserve MonadState
...

Monad m => MonadReader r (ReaderT r m)
MonadReader instance
MonadIO m => MonadIO (ReaderT r m)
preserve MonadIO
MonadState s m => MonadState s (ReaderT r m)
preserve MonadIO
preserve MonadState
```

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in total

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- allows flexible stacking of monad transformers: choose those transformers that are required for application
- quite some effort to integrate new monad transformer:
 full implementation requires connection to all other abstract classes

Stacking of Monad Transformers Example - Setup

```
data AppConfig = AppConfig {
    cfgMaxDepth :: Int
    } deriving (Show)

data AppState = AppState {
    stDeepestReached :: Int
    } deriving (Show)

type App = ReaderT AppConfig (StateT AppState IO)

runApp :: App a -> Int -> IO (a, AppState)
runApp app maxDepth =
    let config = AppConfig maxDepth
        state = AppState O
    in runStateT (runReaderT app config) state
```

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```
Stacking of Monad Transformers Example – App
```

```
countEntries3Main :: Int -> FilePath -> App [(FilePath, Int)]
 countEntries3Main curDepth path = do
   contents <- liftIO . listDirectory $ path</pre>
   allowedDepth <- cfgMaxDepth <$> ask
   rest <- flip mapM contents $ \name -> do
     let newPath = path </> name
     isDir <- liftIO $ doesDirectorvExist newPath</pre>
     if isDir && curDepth < allowedDepth
       then do
         let newDepth = curDepth + 1
         st <- get
         when (stDeepestReached st < newDepth) $
           put $ st { stDeepestReached = newDepth }
         countEntries3Main newDepth newPath
       else return []
   return $ (path, length contents) : concat rest
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```

Final Steps

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wrapper for application that removes App type

```
countEntries3Main :: Int -> FilePath -> App [(FilePath, Int)]
runApp :: App a -> Int -> IO (a, AppState)

countEntries3 :: Int -> FilePath -> IO ([(FilePath, Int)], Int)
countEntries3 md fp =
  second stDeepestReached <$> runApp (countEntries3Main O fp) md
```

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Limits of MTL

- when using MTL, one often can just use all features of the transformers in the stack
- there are two major exceptions
 - a single transformer occurs multiple times, e.g., StateT Int (StateT String IO)
 - what should be the type of get? return an Int or a String? how to access the other state?
 - monads outside MTL are used, where no automatic instance forwarding is available
 - example problem

```
class Monad m => MyMonad m where
  myFun :: Int -> a -> m [a]

foo :: MyMonad m => a -> ReaderT Int m a
foo x = do
  i <- ask
  {- how to invoke "xs <- myFun i x" at this point? -}
  return $ xs !! max i 5</pre>
```

• both problems can be solved by using

```
lift :: (MonadTrans t, Monad m) => m a -> t m a
```

- using lift, we get access to monad operations that are one level deeper in the stack
- most (or even all) monad transformers in MTL instantiate MonadTrans

```
MonadTrans and lift :: (MonadTrans t, Monad m) => m a -> t m a

• second problem solved
   class Monad m => MyMonad m where myFun :: Int -> a -> m [a]
   foo :: MyMonad m => a -> ReaderT Int m a
   foo x = do
        i <- ask
        xs <- lift $ myFun i x
        return $ xs !! max i 5
        • here, myFun i x :: m [a], so lift $ myFun i x :: ReaderT Int m [a]

• first problem solved
   bar :: StateT Int (StateT String IO) ()
   bar = do</pre>
```

-- outer StateT

(x :: Int) <- read <\$> liftIO getLine

(s :: String) <- lift \$ get -- inner StateT

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put x

liftIO \$ putStrLn s

Design Decision

- in second problem from previous slide, one has two alternatives
- solution via lift
 - advantage: no instance declarations are required
 - disadvantage: application code needs to insert lift
- solution by writing instance declarations
 - disadvantage: a lot of boilerplate code has to be written $(n \times n \text{ problem})$
 - advantage: more comfort for the user fewer manual liftings
- preferable solutions depends on number of required liftings

Literature

• Real World Haskell, Chapters 16 and 18

