# Lecture Notes in Artificial Intelligence 9195

#### Subseries of Lecture Notes in Computer Science

LNAI Series Editors

Randy Goebel University of Alberta, Edmonton, Canada Yuzuru Tanaka Hokkaido University, Sapporo, Japan Wolfgang Wahlster DFKI and Saarland University, Saarbrücken, Germany

#### LNAI Founding Series Editor

Joerg Siekmann DFKI and Saarland University, Saarbrücken, Germany More information about this series at http://www.springer.com/series/1244

Amy P. Felty · Aart Middeldorp (Eds.)

# Automated Deduction – CADE-25

25th International Conference on Automated Deduction Berlin, Germany, August 1–7, 2015 Proceedings



*Editors* Amy P. Felty University of Ottawa Ottawa Canada

Aart Middeldorp University of Innsbruck Innsbruck Austria

ISSN 0302-9743 ISSN 1611-3349 (electronic) Lecture Notes in Artificial Intelligence ISBN 978-3-319-21400-9 ISBN 978-3-319-21401-6 (eBook) DOI 10.1007/978-3-319-21401-6

Library of Congress Control Number: 2015943367

LNCS Sublibrary: SL7 - Artificial Intelligence

Springer Cham Heidelberg New York Dordrecht London

© Springer International Publishing Switzerland 2015

This work is subject to copyright. All rights are reserved by the Publisher, whether the whole or part of the material is concerned, specifically the rights of translation, reprinting, reuse of illustrations, recitation, broadcasting, reproduction on microfilms or in any other physical way, and transmission or information storage and retrieval, electronic adaptation, computer software, or by similar or dissimilar methodology now known or hereafter developed.

The use of general descriptive names, registered names, trademarks, service marks, etc. in this publication does not imply, even in the absence of a specific statement, that such names are exempt from the relevant protective laws and regulations and therefore free for general use.

The publisher, the authors and the editors are safe to assume that the advice and information in this book are believed to be true and accurate at the date of publication. Neither the publisher nor the authors or the editors give a warranty, express or implied, with respect to the material contained herein or for any errors or omissions that may have been made.

Printed on acid-free paper

Springer International Publishing AG Switzerland is part of Springer Science+Business Media (www.springer.com)

#### Preface

This volume contains the papers presented at the 25th Jubilee Edition of the International Conference on Automated Deduction (CADE-25), held August 1–7, 2015, in Berlin, Germany. CADE is the major forum for the presentation of research in all aspects of automated deduction, including foundations, applications, implementations, and practical experience.

The Program Committee (PC) accepted 36 papers (24 full papers and 12 system descriptions) out of a total of 85 submissions. Each submission was reviewed by at least three PC members or external reviewers appointed by the PC members in charge. The program also included invited lectures given by Ulrich Furbach (University of Koblenz, Germany) and Edward Zalta (Stanford University, USA). In addition, Michael Genesereth (Stanford University, USA) gave an invited lecture in conjunction with the co-located event RuleML (9th International Web Rule Symposium).

To celebrate the 25th jubilee edition of the conference, additional invited speakers were featured at several events. A Special Session on the Past, Present, and Future of Automated Deduction included talks by Ursula Martin (University of Oxford, UK), Frank Pfenning (Carnegie Mellon University, USA), David Plaisted (University of North Carolina at Chapel Hill, USA), and Andrei Voronkov (University of Manchester, UK). Also, the conference reception and the banquet dinner featured speakers Wolfgang Bibel and Jörg Siekmann. In addition, the program was enriched by several affiliated events that took place before the main conference. These events included eight workshops, seven tutorials, three competitions, and one poster event.

During the conference, the Herbrand Award for Distinguished Contributions to Automated Reasoning was presented to Andrei Voronkov in recognition of his numerous theoretical and practical contributions to automated deduction and the development of the award-winning Vampire theorem prover. The Selection Committee for the Herbrand Award consisted of the CADE-25 Program Committee members, the trustees of CADE Inc., and the Herbrand Award winners of the last ten years.

The Best Paper Award was conferred to Vijay D'Silva (Google, Inc., USA) and Caterina Urban (École Normale Supérieure, France) for their paper entitled "Abstract Interpretation as Automated Deduction." In addition, the first Thoralf Skolem Awards were conferred this year to reward CADE papers that have passed the test of time by being most influential papers in the field:

**CADE-20** (2005) Nominal techniques in Isabelle/HOL by Christian Urban and Christine Tasson: The first paper showing how to use nominal techniques to deal with bound variables in higher-order theorem provers.

**CADE-14 (1997)** SATO: An Efficient Propositional Prover by Hantao Zhang: For its seminal contribution to the design and implementation of novel techniques, including lazy data structures and clever Boolean constraint propagation that caused a step change in the area and deeply influenced later systems.

**CADE-8** (1986) Commutation, Transformation, and Termination by Leo Bachmair and Nachum Dershowitz: For laying the foundations of today's termination theorem-proving techniques.

**CADE-0-1** (1968 and 1975) The mathematical language AUTOMATH, its usage, and some of its extensions by N.G. de Bruijn: For his landmark and remarkable contribution to the design and implementation of higher-order theorem provers.

Also, several students received Woody Bledsoe Travel Awards, thus named to remember the late Woody Bledsoe, funded by CADE Inc. to sponsor student participation.

Many people contributed to making CADE-25 a success. We are very grateful to the members of the Program Committee and the external reviewers for carefully reviewing and evaluating papers. CADE-25 would not have been possible without the dedicated work of the Organizing Committee, headed by Conference Chair Christoph Benzmüller. Many thanks also go to Workshop, Tutorial, and Competition Co-chairs Jasmin Blanchette and Andrew Reynolds, and to Publicity and Web Chair Julian Röder. On behalf of the Program Committee, we also thank all the invited speakers for their contribution to the success of this jubilee edition. We also acknowledge the important contributions of the workshop organizers, tutorial speakers, competition organizers, and poster event organizer. Thanks also go to Andrei Voronkov and the development team of the EasyChair system. Last, but not least, we thank all authors who submitted papers to CADE-25 and all participants of the conference.

CADE-25 received support from many organizations. On behalf of all organizers, we thank the German Research Foundation, DFG, for supporting the special session, and the European Coordinating Committee for Artificial Intelligence (ECCAI) for supporting the invited talk given by Ulrich Furbach. We also gratefully acknowledge support from Freie Universität Berlin, the *Artificial Intelligence Journal*, and Microsoft Research.

May 2015

Amy P. Felty Aart Middeldorp

# **Affiliated Events**

#### Workshops

- Bridging: Bridging the Gap Between Human and Automated Reasoning, organized by Ulrich Furbach, Natarajan Shankar, Marco Ragni, and Steffen Hölldobler
- DT: 29. Jahrestreffen der GI-Fachgruppe Deduktionssysteme, organized by Christoph Benzmüller, Matthias Horbach, Alexander Steen, and Max Wisniewski
- HOL4: HOL4 Workshop, organized by Ramana Kumar
- IWC: Fourth International Workshop on Confluence, organized by Takahito Aoto and Ashish Tiwari
- LFMTP: International Workshop on Logical Frameworks and Meta-Languages: Theory and Practice, organized by Kaustuv Chaudhuri and Iliano Cervesato
- PxTP: Workshop on Proof eXchange for Theorem Proving, organized by Cezary Kaliszyk and Andrei Paskevich
- QUANTIFY: Second International Workshop on Quantification, organized by Hubie Chen, Florian Lonsing, and Martina Seidl
- Vampire: The Vampire Workshop, organized by Laura Kovacs and Andrei Voronkov

#### Tutorials

- Abella: Reasoning About Computational Systems Using Abella, given by Kaustuv Chaudhuri and Gopalan Nadathur
- Beluga: Programming Proofs About Formal Systems, given by Brigitte Pientka
- CPROVER: From Programs to Logic: The CPROVER Verification Tools, given by Daniel Kroening, Martin Brain, and Peter Schrammel
- Isabelle: Isabelle Tutorial, given by Makarius Wenzel
- KeY: The Sequent Calculus of the KeY Tool, given by Reiner H\u00e4hnle and Peter Schmitt
- Lean: Lean Theorem Prover: A Tutorial, given by Leonardo de Moura, Soonho Kong, Jeremy Avigad, and Floris van Doorn
- Superposition: 25th Anniversary of Superposition: Status and Future, given by Stephan Schulz and Christoph Weidenbach

# Competitions

- CoCo: The Fourth Confluence Competition, organized by Takahito Aoto, Nao Hirokawa, Julian Nagele, Naoki Nishida, and Harald Zankl
- CASC: The CADE ATP System Competition, organized by Geoff Sutcliffe
- termCOMP: Termination Competition, organized by Johannes Waldmann and Stefan von der Krone

VIII Affiliated Events

#### **Poster Events**

 EPS: The CADE-25 Taskforce Towards an Encyclopedia of Proof Systems, organized by Bruno Woltzenlogel Paleo

# Organization

# **Program Chairs**

Amy Felty	University of Ottawa, Canada
Aart Middeldorp	University of Innsbruck, Austria

# **Program Committee**

Carlos Areces Alessandro Armando	Universidad Nacional de Córdoba, Argentina University of Genova, Italy
Christoph Benzmüller	Freie Universität Berlin, Germany
Josh Berdine	Microsoft Research, UK
Jasmin Blanchette	Inria Nancy and LORIA, France
Marta Cialdea Mayer	Università di Roma Tre, Italy
Stephanie Delaune	CNRS, France
Gilles Dowek	Inria, France
Amy Felty	University of Ottawa, Canada
Reiner Hähnle	Technical University of Darmstadt, Germany
Stefan Hetzl	Vienna University of Technology, Austria
Marijn Heule	The University of Texas at Austin, USA
Nao Hirokawa	JAIST, Japan
Ullrich Hustadt	University of Liverpool, UK
Deepak Kapur	University of New Mexico, USA
Gerwin Klein	NICTA and UNSW, Australia
Laura Kovacs	Chalmers University of Technology, Sweden
Carsten Lutz	Universität Bremen, Germany
Assia Mahboubi	Inria, France
Aart Middeldorp	University of Innsbruck, Austria
Albert Oliveras	Technical University of Catalonia, Spain
Nicolas Peltier	CNRS, France
Brigitte Pientka	McGill University, Canada
Ruzica Piskac	Yale University, USA
André Platzer	Carnegie Mellon University, USA
Andrew Reynolds	EPFL Lausanne, Switzerland
Christophe Ringeissen	LORIA-Inria, France
Renate A. Schmidt	University of Manchester, UK
Stephan Schulz	DHBW Stuttgart, Germany
Georg Struth	University of Sheffield, UK
Geoff Sutcliffe	University of Miami, USA

Alwen Tiu	Nanyang Technological University, Singapore
Freek Wiedijk	Radboud University Nijmegen, The Netherlands

# **Conference Chair**

Christoph Benzmüller F	reie Universität Berlin, Germany
------------------------	----------------------------------

#### Workshop, Tutorial, and Competition Co-chairs

Jasmin Blanchette	Inria Nancy and LORIA, France
Andrew Reynolds	EPFL Lausanne, Switzerland

# **Publicity and Web Chair**

Julian Röder Fr	eie Universität Berlin, Germany
-----------------	---------------------------------

#### **Additional Reviewers**

Albarghouthi, Aws	Galmiche, Didier	Klebanov, Vladimir
Alberti, Francesco	Gao, Sicun	Klein, Dominik
Andronick, June	Ghilardi, Silvio	Kneuss, Etienne
Avanzini, Martin	Ghorbal, Khalil	Koenighofer, Robert
Balbiani, Philippe	Gieseke, Fabian	Kontchakov, Roman
Bard, Gregory	Giesl, Jürgen	Krishna, Siddharth
Basold, Henning	Gimenez, Stéphane	Kyas, Marcel
Baumgartner, Peter	Goré, Rajeev	Lange, Martin
Bjørner, Nikolaj	Griggio, Alberto	Le Berre, Daniel
Bonacina, Maria Paola	Gupta, Ashutosh	Lee, Matias David
Boy de La Tour, Thierry	Habermehl, Peter	Lewis, Corey
Bubel, Richard	Hansen, Peter	Limongelli, Carla
Cerrito, Serenella	Henriques, David	Lombardi, Henric
Chaudhuri, Kaustuv	Hermant, Olivier	Martins, João G.
Cohen, Cyril	Hladik, Jan	Matichuk, Daniel
David, Amélie	Horbach, Matthias	McMillan, Ken
Demri, Stéphane	Huisman, Marieke	Murray, Toby
Dima, Catalin	Ibanez-Garcia,	Müller, Andreas
Dimitrova, Rayna	Yazmin Angelica	Nadathur, Gopalan
van Ditmarsch, Hans	Iosif, Radu	Nalon, Cláudia
Dragan, Ioan	Jeannin, Jean-Baptiste	Niksic, Filip
Echahed, Rachid	Johansson, Moa	de Nivelle, Hans
Echenim, Mnacho	Jovanović, Dejan	Orbe, Ezequiel
Emmi, Michael	Junttila, Tommi	Papacchini, Fabio
Felgenhauer, Bertram	Kaliszyk, Cezary	Park, Sungwoo
Fontaine, Pascal	Kaminski, Mark	Paskevich, Andrei
Fuhs, Carsten	King, Tim	Peñaloza, Rafael

Popescu, Andrei	Steen, Alexander	Wasser, Nathan
Pous, Damien	Stratulat, Sorin	Weber, Tjark
Qiu, Xiaokang	Suda, Martin	Weller, Daniel
Ranise, Silvio	Thiemann, René	Windsteiger, Wolfgang
Reger, Giles	Théry, Laurent	Wisniewski, Max
Riener, Martin	Tiwari, Ashish	Woltzenlogel Paleo,
Rushby, John	Tourret, Sophie	Bruno
Saurin, Alexis	Traytel, Dmitriy	Zantema, Hans
Sebastiani, Roberto	Urban, Josef	Zawadzki, Erik
Seidl, Martina	Valiron, Benoît	Zeilberger, Noam
Sibut-Pinote, Thomas	Völp, Marcus	Zilani, Beta
Silva, Alexandra	Waldmann, Uwe	Zufferey, Damien

#### 2015 Thoralf Skolem Award Committee

Alessandro Armando	University of Genova, Italy
Gilles Barthe	IMDEA Software Institute, Spain
Claude Kirchner (Chair)	Inria, France
Christopher Lynch	Clarkson University, USA
Leonardo de Moura	Microsoft Research, USA
Uli Sattler	University of Manchester, UK
Geoff Sutcliffe	University of Miami, USA
Toby Walsh	NICTA, Australia
Christoph Weidenbach	Max Planck Institute for Informatics, Germany

#### **Board of Trustees of CADE Inc.**

Peter Baumgartner	NICTA and ANU, Australia
Maria Paola Bonacina	University of Verona, Italy
(President)	
Amy Felty (PC Co-chair)	University of Ottawa, Canada
Pascal Fontaine	University of Lorraine and LORIA, France
Martin Giese (Secretary)	University of Oslo, Norway
Jürgen Giesl	RWTH Aachen, Germany
Neil Murray (Treasurer)	University at Albany, SUNY, USA
Larry Paulson	University of Cambridge, UK
Brigitte Pientka	McGill University, Canada
Renate A. Schmidt	University of Manchester, UK
(Vice-President)	
Geoff Sutcliffe	University of Miami, USA
Christoph Weidenbach	Max Planck Institute for Informatics, Germany

#### Board of the Association for Automated Reasoning

Jasmin Blanchette (Newsletter Editor)	Inria Nancy and LORIA, France
Pascal Fontaine (CADE)	University of Lorraine and LORIA, France
Martin Giese (Secretary)	University of Oslo, Norway
Hans Jürgen Ohlbach	LMU Munich, Germany
(Vice-President)	
Renate Schmidt (CADE)	University of Manchester, UK
Larry Wos (President)	Argonne National Laboratory, USA

#### **Sponsors**

The CADE conference series is sponsored by CADE Inc., a sub-corporation of the Association for Automated Reasoning. In addition, CADE-25 gratefully acknowledges support from Freie Universität Berlin, the *Artificial Intelligence Journal*, Microsoft Research, the German Research Foundation, DFG, and the European Coordinating Committee for Artificial Intelligence.

# **Abstracts of Invited Talks**

The first three abstracts are for invited talks given in the Special Session on the Past, Present, and Future of Automated Deduction. The next three are for those given during the main conference. These are followed by three abstracts describing the competitions held at CADE-25.

# History and Prospects for First-Order Automated Deduction

David A. Plaisted

352 Sitterson Hall Department of Computer Science, UNC Chapel Hill Chapel Hill, NC, 27599-3175, USA http://www.cs.unc.edu/~plaisted

On the fiftieth anniversary of the appearance of Robinson's resolution paper [1], it is appropriate to consider the history and status of theorem proving, as well as its possible future directions. Here we discuss the history of first-order theorem proving both before and after 1965, with some personal reflections. We then generalize model-based reasoning to first-order provers, and discuss what it means for a prover to be goal sensitive. We also present a way to analyze asymptotically the size of the search space of a first-order prover in terms of the size of a minimal unsatisfiable set of ground instances of a set of first-order clauses.

#### Reference

1. Robinson, J.: A machine-oriented logic based on the resolution principle. J. ACM 12(1), 23–41 (1965)

# On the Role of Proof Theory in Automated Deduction

Frank Pfenning

Carnegie Mellon University, USA

Since the seminal work by Gentzen, who developed both natural deduction and the sequent calculus, there has been a line of research concerned with discovering deep structural properties of proofs in order to control the search space in theorem proving. This is particularly important in non-classical logics where traditional model-theoretic techniques may be more difficult to apply. We will walk through some of the key developments, starting with cut elimination and identity expansion, followed by focusing, polarization, and the separation of judgments and propositions. These concepts have been surprisingly robust, applicable to many non-classical logics, to the extent that one may consider them a litmus test on whether a set of rules or axioms form a coherent logic. We illustrate how each of these ideas affect proof search. In some cases, proofs are sufficiently restricted so that proof search can be seen as a fundamental computational mechanism, giving rise to logic programming.

# Stumbling Around in the Dark: Lessons from Everyday Mathematics

Ursula Martin

University of Oxford, UK Ursula.Martin@cs.ox.ac.uk

The growing use of the internet for collaboration, and of numeric and symbolic software to perform calculations it is impossible to do by hand, not only augment the capabilities of mathematicians, but also afford new ways of observing what they do. In this essay we look at four case studies to see what we can learn about the everyday practice of mathematics: the *polymath* experiments for the collaborative production of mathematics, which tell us about mathematicians attitudes to working together in public; the *minipolymath* experiments in the same vein, from which we can examine in finer grained detail the kinds of activities that go on in developing a proof; the mathematical-research-in-the-small; and finally the role of computer algebra, in particular the GAP system, in the production of mathematics. We conclude with perspectives on the role of computational logic.

# Automated Reasoning in the Wild

Ulrich Furbach, Björn Pelzer, and Claudia Schon

Universität Koblenz-Landau, Germany {uli, bpelzer, schon}@uni-koblenz.de

This paper discusses the use of first order automated reasoning in question answering and cognitive computing. For this the natural language question answering project LogAnswer is briefly depicted and the challenges faced therein are addressed. This includes a treatment of query relaxation, web-services, large knowledge bases and co-operative answering. In a second part a bridge to human reasoning as it is investigated in cognitive psychology is constructed by using standard deontic logic.

Work supported by DFG FU 263/15-1 'Ratiolog'.

#### **The Herbrand Manifesto**

#### Thinking Inside the Box

Michael Genesereth and Eric J.Y. Kao

Computer Science Department Stanford University, USA genesereth@stanford.edu erickao@cs.stanford.edu

The traditional semantics for (first-order) relational logic (sometimes called *Tarskian* semantics) is based on the notion of interpretations of constants in terms of objects external to the logic. *Herbrand* semantics is an alternative that is based on truth assignments for ground sentences without reference to external objects. Herbrand semantics is simpler and more intuitive than Tarskian semantics; and, consequently, it is easier to teach and learn.

Moreover, it is more expressive than Tarskian semantics. For example, while it is not possible to finitely axiomatize natural number arithmetic completely with Tarskian semantics, this can be done easily with Herbrand semantics. Herbrand semantics even enables us to define the least fixed-point model of a stratified logic program without any special constructs.

The downside is a loss of some familiar logical properties, such as compactness and proof-theoretic completeness. However, there is no loss of inferential power—anything that can be deduced according to Tarskian semantics can also be deduced according to Herbrand semantics.

Based on these results, we argue that there is value in using Herbrand semantics for relational logic in place of Tarskian semantics. It alleviates many of the current problems with relational logic and ultimately may foster a wider use of relational logic in human reasoning and computer applications. To this end, we have already taught several sessions of the computational logic course at Stanford and a popular MOOC using Herbrand semantics, with encouraging results in both cases.

#### Automating Leibniz's Theory of Concepts

Jesse Alama<sup>1</sup>, Paul E. Oppenheimer<sup>2</sup>, and Edward N. Zalta<sup>2</sup>

Our computational metaphysics group describes its use of automated reasoning tools to study Leibniz's theory of concepts. We start with a reconstruction of Leibniz's theory within the theory of abstract objects (henceforth 'object theory'). Leibniz's theory of concepts, under this reconstruction, has a nonmodal algebra of concepts, a concept-containment theory of truth, and a modal metaphysics of complete individual concepts. We show how the object-theoretic reconstruction of these components of Leibniz's theory can be represented for investigation by means of automated theorem provers and finite model builders. The fundamental theorem of Leibniz's theory is derived using these tools.

# **Confluence Competition 2015**

Takahito Aoto<sup>1</sup>, Nao Hirokawa<sup>2</sup>, Julian Nagele<sup>3</sup>, Naoki Nishida<sup>4</sup>, and Harald Zankl<sup>3</sup>

<sup>1</sup> Tohoku University, Japan
<sup>2</sup> JAIST, Japan
<sup>3</sup> University of Innsbruck, Austria
<sup>4</sup> Nagoya University, Japan

Confluence is one of the central properties of rewriting. Our competition aims to foster the development of techniques for proving/disproving confluence of various formalisms of rewriting automatically. We explain the background and setup of the 4th Confluence Competition.

# The CADE-25 ATP System Competition CASC-25

Geoff Sutcliffe

University of Miami, USA

The CADE ATP System Competition (CASC) is an annual evaluation of fully automatic Automated Theorem Proving (ATP) systems for classical logic the world championship for such systems. One purpose of CASC is to provide a public evaluation of the relative capabilities of ATP systems. Additionally, CASC aims to stimulate ATP research, motivate development and implementation of robust ATP systems that are useful and easily deployed in applications, provide an inspiring environment for personal interaction between ATP researchers, and expose ATP systems within and beyond the ATP community. Fulfillment of these objectives provides insight and stimulus for the development of more powerful ATP systems, leading to increased and more effective use.

CASC-25 was held on 4th August 2015 as part of the 25th International Conference on Automated Deduction (CADE-25), run on computers supplied by the StarExec project. The CASC-25 web site provides access to all systems and competition resources: http://www.tptp.org/CASC/25.

CASC is run in divisions according to problem and system characteristics. For CASC-25 the divisions were:

- THF: Typed Higher-order Form theorems (axioms with a provable conjecture).
- THN: Typed Higher-order form Non-theorems (axioms with a countersatisfiable conjecture, and satisfiable axiom sets). This division was new for CASC-25.
- TFA: Typed First-order with Arithmetic theorems (axioms with a provable conjecture).
- TFN: Typed First-order with arithmetic Non-theorems (axioms with a countersatisfiable conjecture, and satisfiable axiom sets). This division was new for CASC-25.
- FOF: First-Order Form theorems (axioms with a provable conjecture).
- FNT: First-order form syntactically non-propositional Non-Theorems (axioms with a countersatisfiable conjecture, and satisfiable axiom sets).
- EPR: Effectively PRopositional clause normal form (non-)theorems.
- LTB: First-order form theorems (axioms with a provable conjecture) from Large Theories, presented in Batches with a shared time limit.

Problems for CASC are taken from the TPTP Problem Library. The TPTP version used for CASC is released after the competition, so that new problems have not been seen by the entrants. The THF, TFA, FOF, FNT, and LTB divisions were ranked according to the number of problems solved with an acceptable proof/model output. The THN, TFN, and EPR divisions were ranked according to the number of problems solved, but not necessarily accompanied by a proof or model. Ties are broken according to the average time over problems solved. Division winners are announced and prizes are awarded.

The design and organization of CASC has evolved over the years to a sophisticated state. Decisions made for CASC (alongside the TPTP, and the ES\* series of workshops) have influenced the direction of development in ATP for classical logic. CASC-25 was the 20<sup>th</sup> edition of CASC, and it is interesting to look back on some of the key decisions that have helped bring ATP to its current state.

- CASC-13, 1996: The first CASC stimulated research towards robust, fully automatic systems that take only logical formulae as input. It increased the visibility of systems and developers, and rewarded implementation efforts.
- CASC-14, 1997: Introduced the SAT division, stimulating the development of model finding systems for CNF.
- CASC-15, 1998: Introduced the FOF division, starting the slow demise of CNF to becoming just the "assembly language" of ATP.
- CASC-16, 1999: Changes to the problem selection motivated the development of techniques for automatic tuning of ATP systems' search parameters.
- CASC-JC, 2001: Introduced ranking based on proof output, starting the the trend towards ATP systems that efficiently output proofs and models. Introduced the EPR division, stimulating the development of specialized techniques for this important subclass of problems.
- CASC-20, 2005: Required systems to develop builtin equality reasoning, by removing the equality axioms from the TPTP problems.
- CASC-J3, 2006: The FOF division was promoted as the most important, stimulating development of ATP systems for full first-order logic.
- CASC-21, 2007: Introduced the FNT division, further stimulating the development of model finding systems.
- CASC-J4, 2008: Introduced the LTB division, leading to the development of techniques for automatically dealing with very large axiom sets.
- CASC-J5, 2010: Introduced the THF division, stimulating development of ATP systems for higher-order logic.
- CASC-23, 2011: Introduced the TFA division, stimulating development of ATP systems for full first-order logic with arithmetic.
- CASC-J6, 2012: Otter replaced by Prover9 as the "fixed-point" in the FOF division, demonstrating the progress in ATP.
- CASC-24, 2013: Removed the CNF division, confirming the demise of CNF.
- CASC-J7, 2014: Required use of the SZS ontology, so the ATP systems unambiguously report what they have established about the input.
- CASC-25, 2015: Introduced the THN and TFN divisions, stimulating development of model finding for the TFA and THF logics.

The ongoing success and utility of CASC depends on ongoing contributions of problems to the TPTP. The automated reasoning community is encouraged to continue making contributions of all types of problems.

#### **Termination Competition (termCOMP 2015)**

Jürgen Giesl<sup>1</sup>, Frédéric Mesnard<sup>2</sup>, Albert Rubio<sup>3</sup>, René Thiemann<sup>4</sup>, and Johannes Waldmann<sup>5</sup>

<sup>1</sup> RWTH Aachen University, Germany
<sup>2</sup> Université de la Réunion, France
<sup>3</sup> Universitat Politècnica de Catalunya - BarcelonaTech, Spain
<sup>4</sup> Universität Innsbruck, Austria
<sup>5</sup> HTWK Leipzig, Germany

The termination competition focuses on automated termination analysis for all kinds of programming paradigms, including categories for term rewriting, imperative programming, logic programming, and functional programming. Moreover, the competition also features categories for automated complexity analysis. In all categories, the competition also welcomes the participation of tools providing certified proofs. The goal of the termination competition is to demonstrate the power of the leading tools in each of these areas.

(project DAMAS).

F. Giesl—This author is supported by the Deutsche Forschungsgemeinschaft (DFG) grant GI 274/6-1. A. Rubio—This author is supported by the Spanish MINECO under the grant TIN2013-45732- C4-3-P

R. Thiemann-This author is supported by the Austrian Science Fund (FWF) project Y757.

# Contents

Past, Present and Future of Automated Deduction	
History and Prospects for First-Order Automated Deduction	3
Stumbling Around in the Dark: Lessons from Everyday Mathematics Ursula Martin	29
Invited Talks	
Automated Reasoning in the Wild Ulrich Furbach, Björn Pelzer, and Claudia Schon	55
Automating Leibniz's Theory of Concepts Jesse Alama, Paul E. Oppenheimer, and Edward N. Zalta	73
Competition Descriptions	
Confluence Competition 2015 Takahito Aoto, Nao Hirokawa, Julian Nagele, Naoki Nishida, and Harald Zankl	101
Termination Competition (termCOMP 2015) Jürgen Giesl, Frédéric Mesnard, Albert Rubio, René Thiemann, and Johannes Waldmann	105
Rewriting	
Non-E-Overlapping, Weakly Shallow, and Non-Collapsing TRSs Are Confluent	111
CoLL: A Confluence Tool for Left-Linear Term Rewrite Systems	127
Term Rewriting with Prefix Context Constraints and Bottom-Up Strategies Florent Jacquemard, Yoshiharu Kojima, and Masahiko Sakai	137
Encoding Dependency Pair Techniques and Control Strategies for Maximal Completion	152

Reducing Relative Termination to Dependency Pair Problems José Iborra, Naoki Nishida, Germán Vidal, and Akihisa Yamada	163
Decision Procedures	
Decidability of Univariate Real Algebra with Predicates for Rational and Integer Powers <i>Grant Olney Passmore</i>	181
A Decision Procedure for (Co)datatypes in SMT Solvers Andrew Reynolds and Jasmin Christian Blanchette	197
Deciding ATL* Satisfiability by Tableaux	214
Interactive/Automated Theorem Proving and Applications	
A Formalisation of Finite Automata Using Hereditarily Finite Sets Lawrence C. Paulson	231
SEPIA: Search for Proofs Using Inferred Automata Thomas Gransden, Neil Walkinshaw, and Rajeev Raman	246
Proving Correctness of a KRK Chess Endgame Strategy by Using Isabelle/HOL and Z3 <i>Filip Marić, Predrag Janičić, and Marko Maliković</i>	256
Inductive Beluga: Programming Proofs Brigitte Pientka and Andrew Cave	272
New Techniques for Automating and Sharing Proofs	
SMTtoTPTP – A Converter for Theorem Proving Formats Peter Baumgartner	285
CTL Model Checking in Deduction Modulo	295
Quantifier-Free Equational Logic and Prime Implicate Generation	311
Quantomatic: A Proof Assistant for Diagrammatic Reasoning Aleks Kissinger and Vladimir Zamdzhiev	326
Automating First-Order Logic	
Cooperating Proof Attempts	339

Giles Reger, Dmitry Tishkovsky, and Andrei Voronkov

Contents	XXVII

Towards the Compression of First-Order Resolution Proofs by Lowering Unit Clauses	356
Beagle – A Hierarchic Superposition Theorem Prover Peter Baumgartner, Joshua Bax, and Uwe Waldmann	367
The Lean Theorem Prover (System Description) Leonardo de Moura, Soonho Kong, Jeremy Avigad, Floris van Doorn, and Jakob von Raumer	378
System Description: E.T. 0.1 Cezary Kaliszyk, Stephan Schulz, Josef Urban, and Jiří Vyskočil	389
Playing with AVATAR Giles Reger, Martin Suda, and Andrei Voronkov	399
Combinations	
A Polite Non-Disjoint Combination Method: Theories with Bridging Functions Revisited Paula Chocron, Pascal Fontaine, and Christophe Ringeissen	419
Exploring Theories with a Model-Finding Assistant	434
Abstract Interpretation as Automated Deduction Vijay D'Silva and Caterina Urban	450
Hybrid Sytoms and Drogram Synthesis	

#### Hybrid Sytems and Program Synthesis

A Uniform Substitution Calculus for Differential Dynamic Logic André Platzer	467
Program Synthesis Using Dual Interpretation Ashish Tiwari, Adrià Gascón, and Bruno Dutertre	482

#### Logics and Systems for Program Verification

Automated Theorem Proving for Assertions in Separation Logic	
with All Connectives	501
Zhé Hóu, Rajeev Goré, and Alwen Tiu	
KeY-ABS: A Deductive Verification Tool for the Concurrent Modelling Language ABS	517

Contents

KeYmaera X: An Axiomatic Tactical Theorem Prover for Hybrid Systems Nathan Fulton, Stefan Mitsch, Jan-David Quesel, Marcus Völp, and André Platzer	527
Tableaux Methods for Propositional Dynamic Logics with SeparatingParallel CompositionPhilippe Balbiani and Joseph Boudou	539
Unification	
Regular Patterns in Second-Order Unification	557
Theorem Proving with Bounded Rigid <i>E</i> -Unification <i>Peter Backeman and Philipp Rümmer</i>	572
SAT/SMT	
Expressing Symmetry Breaking in DRAT Proofs	591
MathCheck: A Math Assistant via a Combination of Computer Algebra Systems and SAT Solvers Edward Zulkoski, Vijay Ganesh, and Krzysztof Czarnecki	607
Linear Integer Arithmetic Revisited Martin Bromberger, Thomas Sturm, and Christoph Weidenbach	623
Author Index	639